# SPENDING ON SOCIAL WELFARE PROGRAMS IN RICH AND POOR STATES 

Contract \# 282-98-0016
Task Order \#34
Final Report
Appendix A

Prepared for:
Department of Health and Human Services
Assistant Secretary for Planning and
Evaluation

Prepared by:
The Lewin Group
and its subcontractor
The Nelson A. Rockefeller Institute of Government June 3, 2004

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## Table of Contents

APPENDIX A .....  .1
Theoretical Foundations .....  1
Full Model Specifications and Results .....  4

## APPENDIX A

In this Appendix, we set out the theoretical foundation for the 50 -state econometric model and provide more extensive estimates of model parameters.

## Theoretical Foundations

Following McGuire (1978) we develop an empirical model of spending by state and local governments. The decision-makers are assumed to maximize a general utility or preference function defined in terms of public and private goods. Public spending on specified activities is determined in part by the relative marginal social utility placed on that category by the state. Both state fiscal capacity and federal grants become part of the state's budget constraint. Economic conditions within each state are explanatory variables because they determine the relative social utility (or "need") of spending on specified activities.

A Stone-Geary specification for the preference function ${ }^{1}$ leads to a series of linear expenditure functions in which per capita total state and local spending on a specified public function is a function of several explanatory variables, including per capita personal income, per capita federal grants, and a number of variables designed to capture the relative need of the states for social welfare spending.

This type of model allows us to focus on how states with different needs for social welfare spending respond to changes in explanatory variables such as fiscal capacity, and the availability of federal grants. It will also allow us to explore how fiscal capacity itself affects state spending on social welfare and other functions.

Our basic (per capita) budget constraint for spending on a particular category of public activity in the combined state-local system was taken to be the sum of per capita personal income (PCPI) and per capita federal grants for that type of spending. If state-local needs were constant (or independent of the other explanatory variables), and federal grants had only income effects², per capita spending would be a simple linear function of PCPI plus federal grants per capita with a series of dummy variables to represent state effects. That is:

$$
\mathrm{S}=\mathrm{a}+\beta \mathrm{R}+\Sigma \delta_{\mathrm{j}} \mathrm{D}_{\mathrm{j}}+\Sigma \lambda_{\mathrm{k}} \mathrm{X}_{\mathrm{k}}
$$

where $S=$ per capita spending on a particular category of spending
$R=$ per capita resources for spending on that category
$D_{j}=$ a dummy variable having the value 1 if the observation is for the $j$ th state, and 0, otherwise; and

[^0]$\mathrm{X}_{\mathrm{k}}=$ the kth explanatory variable in the equation in addition to per capita resources and the state dummy variables
$$
a+\delta_{j}=\text { the state effect (i.e., variable intercept) for the particular category of spending }
$$

The above model is called a linear expenditure model. The simplest type of model is one in which spending on a particular good as a share of total available resources is constant. For example, if $\alpha+\delta_{j}=\lambda_{k}=0$, for all states and explanatory variables, the model implies that spending on the particular category of public goods is a constant, i.e.,:
$\beta=S / R$
However, in general the share will not be constant across states if state effects are present and if the explanatory variables influence spending decisions. A more general share model posits that it is not the share of the total budget constraint going to a particular function that is constant. Instead, the spending on a particular function in excess of minimum required spending on that function is a constant fraction of the total budget less the resources necessary to meet all minimum required spending. In this version of the model, $\beta$ is still a constant share but it becomes a constant conditional on the values of all the explanatory variables. ${ }^{3}$ See McGuire (1978) and Appendix A to this report for the full specification of a share model in which minimum required levels of spending vary across states and with the values of explanatory variables.

This type of share model with constant state effects picking up variation in minimum needs across states is the simplest of the model versions we use to analyze spending decisions by state and local governments. The model was also expanded to accommodate other factors, the most important of which include: (1) the tendency of federal grants to be more stimulatory than private per capita income, the so-called "flypaper effect," (2) year effects; (3) need effects; and (4) grant price effects.

## Flypaper Effects

The "flypaper effect" refers to the fact that lump sum unconditional federal grants seems to have a larger stimulatory effect on state and local public spending than a corresponding increase in the income of the citizens that reside in the jurisdiction of the recipient government
${ }^{3} \beta=(S-\lambda) /\left(R-R^{*}\right)$ where $R^{*}$ denotes resources necessary to meet minimum required spending needs for all functions, and $\lambda$ is the minimum required spending for the particular function. $R^{*}$ and $\lambda$ vary across states and with the explanatory variables but are constant once the explanatory variables are fixed. On these assumptions, the state effects for any particular function may be written as: $a+\delta_{j}=\lambda-(R-$
$\left.R^{*}\right) \beta$. Thus a state effect for a particular function is high, other things being equal, if the minimum required spending on the particular function $\lambda$ is high, or if the state's resource requirements needed to meet minimum needs for all functions $\mathrm{R}^{*}$ is low relative to available resources. In other words, a state tends to spend more on a particular function if its specific needs for that function are high or if its needs for other functions are relatively low.
(Gramlich 1977; Hines and Thaler, 1995; Gamkhar and Oates, 1996) This contradicts established theory that indicates that lump sum grants to a locality should have allocative and distributive effects no different than if the grant were distributed directly to the residents of the locality (Bradford and Oates, 1971). Empirical research has strongly established the existence of such an effect, at least in response to increases in federal grants.

Theoretical explanations for the "flypaper effect" vary widely. For example, Hines and Thaler (1995) posit explanations ranging from individuals not recognizing the fungibility of money to the median voter bearing a smaller than average fraction of the tax burden.

Our approach to accommodating the flypaper effect was to partition the budget constant independent resource variable $R$ into two variables, one that reflects private per capita income and one that reflects per capita federal grants.

## Year Effects

Year effects refer to the fact that the minimum needs that drive state-local spending decisions may vary from year to year. We dealt with this by specifying models in which we added dummy variables for each year, to effectively shift up and down the intercept term over time to accommodate time variant effects.

## Particular Needs

We also attempted to model the need effects. Instead of allowing minimum needs simply to vary across states through the state effects, we also introduced variables such as poverty, unemployment, population density and percent urban to explore whether or not states behaved as though they had stable needs functions.

## Price Effects

A matching grant under which the federal government agrees to match state spending at some rate effectively lowers the "price" to the state or local decision-maker (in terms of local resources) of directing resources to the aided governmental function For example, if the federal government agrees to pay $\$ 0.60$ for every dollar of state spending on an activity, then the state's cost (in its own resources) to finance $\$ 1$ in spending on that activity has fallen to $\$(1-0.60)$ or \$0.40. ${ }^{4}$
${ }^{4}$ Much of the research reported is on the issue of how strongly this price effect stimulates state spending on aided activities. The literature contrasts non-matching grants, which are thought to have only income effects, with matching grants, which are thought to have both price and income effects. It also discusses revenue sharing which carries no restrictions on how grant monies are to be used with restricted grants that must be used for designated purposes. Revenue-sharing is thought to have a pure income effect, but no price effect. Restricted unmatched grants are thought to have only income effects if the state would spend at least as much as the grant amount in the absence of the grant (so that the restriction is not binding). However, if the grant restriction is binding, the restricted grant has an implied price effect as well as an income effect. In general, an unrestricted revenue-sharing grant to the states would be expected to reduce state spending as the states would use the money to substitute for spending from their

Following McGuire (1978), we attempted to incorporate the "price" effects of grants into the analysis. This was done formally by assuming that some fraction of a grant was effectively unrestricted, i.e., the grant had a pure income effect through the budget constraint, and the remainder of the grant had only a price effect and thus did not enter the budget constraint. This leads to a more complex model structure in which the ratio of federal grants for a particular category of public functions to total state-local spending enter the linear expenditure function interacted with other variables. The full model is specified below. Another simpler approach to take account of price effects is to add year dummy variables to the regression, which was done in Model 1 without formal consideration of price effects. The results for Model 1D are presented also in the text of this report. The combination of year and state effects will capture much of the variation in changes in grant conditions in particular states at particular times.

## Full Model Specifications and Results

Our model is based on the theoretical work by McGuire (1978), in which he modeled state-local spending on education and non-education functions. However, we have certain data problems not present in McGuire's estimation. He estimated his model on Census data that permitted him to have the same level of aggregation in his data on intergovernmental revenues as in his data on state-local spending, and he used a simple two category model of public activities. On the other hand, our challenge was to press the econometric modeling to accommodate five categories of public goods: cash assistance, Medicaid, other social welfare, public hospitals and non-public hospital non-social welfare spending, while the data on intergovernmental revenues used to estimate federal grant levels was available only for "social welfare spending" and "nonsocial welfare" spending.

To accommodate this restriction in the data, we needed to redefine our dependent variable as total state-local spending rather than state-local spending from all sources. Furthermore, McGuire deals with the so-called "flypaper effect," but by a very ad hoc method, namely, he includes an extra parameter in his equations which is not in the preference function. But this is inconsistent with optimization of the preference function and essentially forces an empirical result that allows the effect of private resources and grant resources on state-local spending to be different. We take a slightly different approach and allow the flypaper effect to shift linearly the minimum subsistence level of spending by whether the source of the income is federal grants or private income.

We set forth the model for two public goods first and then generalize it to four public goods, which is the models we use primarily in the report. However, because the mathematics is rather tedious, it is easier to follow if we use the two good model and then explain how it can be extended to four public goods. For two public goods $\left(Q_{S}\right.$, social welfare spending, and $Q_{0}$, nonsocial welfare spending, and a private good Y ), the Stone-Geary function to be maximized is:

[^1]\[

$$
\begin{equation*}
\mathrm{U}=\left(\mathrm{Y}-\lambda_{\mathrm{y}}\right) \beta_{\mathrm{y}}\left(\mathrm{Q}_{\mathrm{s}}-\lambda_{\mathrm{s}}\right) \beta_{\mathrm{s}}\left(\mathrm{Q}_{\mathrm{o}}-\lambda_{\mathrm{O}}\right) \beta_{\mathrm{o}}, \tag{1}
\end{equation*}
$$

\]

where $\lambda_{y}, \lambda_{s}$, and $\lambda_{0}$, are the minimum required spending for private goods, social welfare public goods, and non-social welfare public goods, respectively, and $\beta_{\mathrm{y}}, \beta_{\mathrm{S}}$, and $\beta_{\mathrm{O}}$ are the relative utility parameters of the utility function. Without loss of generality, the $\beta \mathrm{s}$ can be assumed to equal $1 .{ }^{5}$

Relative prices in the economy are assumed to be fixed, but the price of each of the public goods is assumed to be affected by the terms of the federal grant aiding the particular good. If all of a federal grant were to lower the price of spending the effective price would fall from 1 (i.e., one dollar of state-local spending costs one dollar) to 1-M, where M is federal share of total spending, i.e., $M=G / Q$, where $Q$ is total spending on the aided function ( $G+L$ ), and $G$ and $L$ are federal and state-local spending, respectively. In our model, the price of the aided good will be allowed to vary from 1 to 1-M depending on the degree to which grants have price effects or have pure income effects. Specifically, the price of the aided function is stated as

$$
\begin{equation*}
p=1+(\theta-1) M=(L+\theta G) /(L+G) \tag{2}
\end{equation*}
$$

with $\theta$ expected to vary between 1 and 0 . When $\theta=1$ the grant has no effect on price, and $p=1$. When $\theta=0, p=1-M$. The lower the price, the more the states and localities are expected to spend from their own resources on the aided function.

The social preference function is maximized subject to a budget constraint:

$$
\begin{equation*}
R_{\mathrm{T}}=\mathrm{Y}+\mathrm{p}_{\mathrm{s}} \mathrm{Q}_{\mathrm{s}}+\mathrm{p}_{\mathrm{o}} \mathrm{Q}_{\mathrm{O}}=\mathrm{R}_{\mathrm{L}}+\theta_{\mathrm{S}} \mathrm{G}_{\mathrm{S}}+\theta_{\mathrm{o}} \mathrm{G}_{\mathrm{O}^{\prime}} \tag{3}
\end{equation*}
$$

where the price of private goods is assumed to be 1 (i.e., a numeraire), $\mathrm{p}_{\mathrm{S}}$ and $\mathrm{p}_{\mathrm{O}}$ are the prices (as defined in (2)) of social welfare public goods and other public goods, respectively, $\mathrm{R}_{\mathrm{T}}$ is the total public and private resources, $Y$ is spending on private goods, $Q_{S}$ and $Q_{O}$ are total spending (federal, state and local) on social welfare and other public goods, respectively, $\mathrm{G}_{\mathrm{S}}$ and $\mathrm{G}_{\mathrm{O}}$ are federal grants to aid social welfare, and other public functions, respectively, $\theta_{\mathrm{S}}$ and $\theta_{\mathrm{O}}$ are the fractions of federal grants that do not affect prices, for social welfare and non-social welfare functions, respectively, and $R_{\mathrm{L}}$ is state-local own resources.

Maximizing the preference function (2) subject to the budget constraint (3) leads to the following linear expenditure functions:

$$
\begin{align*}
& p_{s} Q_{s}=L_{s}+\theta_{s} G_{S}=-\beta_{\mathrm{s}} \lambda_{\mathrm{y}}+\beta_{\mathrm{s}} R_{T}+\left(1-\beta_{\mathrm{s}}\right) \lambda_{\mathrm{s}} p_{\mathrm{s}}-\beta_{\mathrm{s}} \lambda_{\mathrm{o}} p_{\mathrm{o}}  \tag{4}\\
& \mathrm{p}_{\mathrm{o}} Q_{\mathrm{o}}=L_{\mathrm{o}}+\theta_{\mathrm{o}} G_{\mathrm{O}}=-\beta_{\mathrm{o}} \lambda_{\mathrm{y}}+\beta_{\mathrm{o}} R_{\mathrm{T}}-\beta_{\mathrm{o}} \lambda_{\mathrm{s}} p_{\mathrm{s}}+\left(1-\beta_{\mathrm{o}}\right) \lambda_{\mathrm{o}} p_{\mathrm{o}} \tag{5}
\end{align*}
$$

${ }^{5}$ The $\beta$ parameters in the utility function can be identified from the linear expenditure functions only to a factor of proportionality. Thus, we do not lose any information by assuming that the parameters sum to unity.

The private spending variable $(Y)$ is determined from the budget constraint $R_{T}-p_{S} Q_{S}-p_{o} Q_{O}$ - Y. Solving for Y gives an equation for private spending similar to the two public spending equations:

$$
\begin{equation*}
Y=R_{L}-L_{S}-L_{O}=\left(1-\beta_{y}\right) \lambda_{y}+\beta_{y} R_{T}-\beta_{y} \lambda_{\mathrm{S}} p_{\mathrm{s}}-\beta_{\mathrm{y}} \lambda_{\mathrm{o}} \mathrm{p}_{\mathrm{o}} \tag{6}
\end{equation*}
$$

Substituting for $\mathrm{R}_{\mathrm{T}}$ from equation (3), for $\mathrm{p}_{\mathrm{S}}$ and $\mathrm{p}_{\mathrm{o}}$ from equation (1), and rearranging terms gives:

$$
\begin{align*}
& \mathrm{L}_{\mathrm{S}}+\mathrm{G}_{\mathrm{S}}=\beta_{\mathrm{S}} \mathrm{R}_{\mathrm{L}}+\beta_{\mathrm{S}} \theta_{\mathrm{O}} \mathrm{G}_{\mathrm{O}}+\beta_{\mathrm{s}} \theta_{\mathrm{S}} \mathrm{G}_{\mathrm{S}}+\left(1-\beta_{\mathrm{s}}\right)\left[1+\left(\theta_{\mathrm{S}}-1\right) \mathrm{M}_{\mathrm{S}}\right] \lambda_{\mathrm{s}} \\
& -\beta_{\mathrm{S}}\left[1+\left(\theta_{\mathrm{O}}-1\right) \mathrm{M}_{\mathrm{o}}\right] \lambda_{\mathrm{o}}-\beta_{\mathrm{s}} \lambda_{\mathrm{y}}  \tag{7}\\
& L_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\beta_{\mathrm{o}} \mathrm{R}_{\mathrm{L}}+\beta_{\mathrm{o}} \theta_{\mathrm{S}} \mathrm{G}_{\mathrm{S}}+\beta_{\mathrm{o}} \theta_{\mathrm{O}} \mathrm{G}_{\mathrm{O}}-\beta_{\mathrm{O}}\left[1+\left(\theta_{\mathrm{S}}-1\right) \mathrm{M}_{\mathrm{S}}\right] \lambda_{\mathrm{S}} \\
& +\left(1-\beta_{\mathrm{O}}\right)\left[1+\left(\theta_{\mathrm{O}}-1\right) \mathrm{M}_{\mathrm{o}}\right] \lambda_{\mathrm{o}}-\beta_{\mathrm{o}} \lambda_{\mathrm{y}}  \tag{8}\\
& Y=\beta_{y} R_{L}+\beta_{y} \theta_{\mathrm{S}} G_{\mathrm{s}}+\beta_{\mathrm{y}} \theta_{\mathrm{o}} \mathrm{G}_{\mathrm{o}}-\beta_{\mathrm{y}}\left[1+\left(\theta_{\mathrm{s}}-1\right) \mathrm{M}_{\mathrm{s}}\right] \lambda_{\mathrm{s}} \\
& -\beta_{\mathrm{y}}\left[1+\left(\theta_{\mathrm{o}}-1\right) \mathrm{M}_{\mathrm{o}}\right] \lambda_{\mathrm{o}}+\left(1-\beta_{\mathrm{y}}\right)_{\mathrm{y}} \tag{9}
\end{align*}
$$

Equations (7), (8), and (9) can be rewritten as reduced form equations linear in the variables $\mathrm{G}_{\mathrm{S}}$, $\mathrm{G}_{\mathrm{O}}, \mathrm{M}_{\mathrm{S}^{\prime}}$ and $\mathrm{M}_{\mathrm{O}}$ :

$$
\begin{align*}
& L_{S}+G_{S}=a_{1}+b_{1} R_{L}+c_{1} G_{O}+d_{1} G_{S}+e_{1} M_{S}+f_{1} M_{o}  \tag{10}\\
& \mathrm{~L}_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2} \mathrm{R}_{\mathrm{L}}+\mathrm{c}_{2} \mathrm{G}_{\mathrm{O}}+\mathrm{d}_{2} \mathrm{G}_{\mathrm{S}}+\mathrm{e}_{2} \mathrm{M}_{\mathrm{S}}+\mathrm{f}_{2} \mathrm{M}_{\mathrm{o}}  \tag{11}\\
& Y=a_{3}+b_{3} R_{L}+c_{3} G_{O}+d_{3} G_{S}+e_{3} M_{S}+f_{3} M_{O} \tag{12}
\end{align*}
$$

where

$$
\begin{aligned}
& \mathrm{a}_{1}=\left(1-\beta_{\mathrm{s}}\right) \lambda_{\mathrm{s}}-\beta_{\mathrm{s}} \lambda_{\mathrm{o}}-\beta_{\mathrm{s}} \lambda_{\mathrm{y}} \\
& \mathrm{a}_{2}=-\beta_{\mathrm{o}} \lambda_{\mathrm{S}}+\left(1-\beta_{\mathrm{O}}\right) \lambda_{\mathrm{o}}-\beta_{\mathrm{o}} \lambda_{\mathrm{y}} \\
& a_{3}=-\beta_{y} \lambda_{\mathrm{S}}-\beta_{\mathrm{y}} \lambda_{\mathrm{o}}+\left(1-\beta_{y} \lambda_{\mathrm{y}} \text { and } \mathrm{a}_{1}+\mathrm{a}_{2}+\mathrm{a}_{3}=0 \text {, since } \beta_{\mathrm{S}}+\beta_{\mathrm{o}}+\beta_{\mathrm{y}}=1\right. \\
& \mathrm{b}_{1}=\beta_{\mathrm{s}} ; \mathrm{b}_{2}=\beta_{\mathrm{o}} ; \text { and } \mathrm{b}_{3}=\beta_{\mathrm{y}} ; \text { and } \mathrm{b}_{1}+\mathrm{b}_{2}+\mathrm{b}_{3}=1 \\
& c_{1}=\beta_{\mathrm{s}} \theta_{\mathrm{O}} ; \quad c_{2}=\beta_{\mathrm{o}} \theta_{\mathrm{o}} ; \mathrm{c}_{3}=\beta_{\mathrm{y}} \theta_{\mathrm{o}} \quad \text { and } \mathrm{c}_{1}+\mathrm{c}_{2}+\mathrm{c}_{3}=\theta_{\mathrm{o}} \\
& d_{1}=\beta_{s} \theta_{\mathrm{s}} ; \quad d_{2}=\beta_{o} \theta_{\mathrm{s}} ; \mathrm{d}_{3}=\beta_{y} \theta_{\mathrm{s}} \quad \text { and } d_{1}+d_{2}+d_{3}=\theta_{\mathrm{s}} \\
& e_{1}=\lambda_{S}\left(1-\beta_{S}\right)\left(\theta_{S}-1\right) ; \quad e_{2}=-\lambda_{S} \beta_{o}\left(\theta_{S}-1\right) \quad ; e_{3}=-\lambda_{s} \beta_{y}\left(\theta_{S}-1\right) \quad \text { and } e_{1}+e_{2}+e_{3}=0
\end{aligned}
$$

$f_{1}=-\lambda_{\mathrm{o}} \beta_{\mathrm{s}}\left(\theta_{\mathrm{o}}-1\right) ; \mathrm{f}_{2}=\lambda_{\mathrm{o}}\left(1-\beta_{\mathrm{o}}\right)\left(\theta_{\mathrm{o}}-1\right) ; \mathrm{f}_{3}=-\lambda_{\mathrm{o}} \beta_{\mathrm{y}}\left(\theta_{\mathrm{o}}-1\right)$ and $\mathrm{f}_{1}+\mathrm{f}_{2}+\mathrm{f}_{3}=0$
We use the above equation as a general model into which we introduce a number of additional restrictions and parameters to test hypotheses.

First, the above model has no flypaper effect because an increase in income affects public spending in the same way whether it arises from local resources or federal grants. The "flypaper effect" refers to the empirical fact that lump sum unconditional federal grants seem to have a larger stimulatory effect on state and local public spending than a corresponding increase in the income of the citizens that reside in the jurisdiction of the recipient government (Gramlich 1977; Hines and Thaler, 1995; Gamkhar and Oates, 1996) This contradicts established theory that indicates that lump sum grants to a locality should have allocative and distributive effects no different than if the grant were distributed directly to the residents of the locality (Bradford and Oates, 1971). Empirical research has strongly established the existence of such an effect, at least in response to increases in federal grants. However, some researchers have found an asymmetric response with the flypaper effect occurring only in response to increases and not in response to decreases in grant levels.

Theoretical explanations for the "flypaper effect" vary widely. For example, Hines and Thaler (1995) posit explanations ranging from individuals not recognizing the fungibility of money to the median voter bearing a smaller than average fraction of the tax burden.

In McGuire's analysis of educational expenditures, he acknowledges the "flypaper effect" by introducing a parameter $\Pi$ assumed to be greater than one that augments the stimulatory effects of federal grants. This parameter enters the linear spending equations multiplicatively and may be interpreted as increasing the "power" of income received through governmental grants. One problem with this approach in the context of McGuire's theoretical model is that it compromises the integrity of his optimization scheme. For example, he begins by positing that state and local decision-makers maximize a Stone-Geary social preference function defined in terms of total spending on various goods (education public good, non-education public goods and private goods). However, when he arbitrarily introduces the new parameter into the demand functions, he can no longer solve the optimization problem for private goods. While his optimization conditions still determine spending on the public goods, the magnitude of the flypaper effect determines the spending on private goods. Ideally, one would incorporate the flypaper effect as a feature of a theoretical optimization model.

We take an approach which allows for optimization with respect to all public and private categories of spending. Instead of arbitrarily increasing the stimulation effect of grants of public spending by a factor $\Pi$, we allow federal grants to affect the minimum required levels of spending for each public good in the model. The grant recipient maximizes a Stone-Geary utility function in which the minimum required spending amounts for each category of public goods is determined by the mix of federal grants and a number of need variables.

Unlike McGuire (1978), we choose to conceptualize the flypaper effect as occurring through the effect of grant income on the minimum required levels of public spending. Because there may be price effects of grants, we need to relate the additional stimulus of a federal grant due to the flypaper effect to the real purchasing power of the grant income if used to fund a specified
category of public spending. Thus, we write the expressions for minimum required public spending levels for social welfare and non-social welfare ( $\lambda_{S}$ and $\lambda_{\mathrm{O}}$, respectively) and the minimum required private spending level $\left(\lambda_{y}\right)$ as:

$$
\begin{align*}
& \lambda_{\mathrm{S}}=\lambda_{\mathrm{s} 0}+\left(\Pi_{\mathrm{OS}} /\left(1+\left(\theta_{\mathrm{S}}-1\right) \mathrm{M}_{\mathrm{s}}\right)\right) \theta_{\mathrm{O}} \mathrm{G}_{\mathrm{O}}+\left(\Pi_{\mathrm{sS}} /\left(1+\left(\theta_{\mathrm{S}}-1\right) \mathrm{M}_{\mathrm{s}}\right)\right) \theta_{\mathrm{S}} \mathrm{G}_{\mathrm{S}}+\sum \lambda_{\mathrm{si}} x_{\mathrm{i}}  \tag{13}\\
& \lambda_{\mathrm{O}}=\lambda_{\mathrm{o} 0}+\left(\Pi_{\mathrm{oO}} /\left(1+\left(\theta_{\mathrm{O}}-1\right) \mathrm{M}_{\mathrm{o}}\right)\right) \theta_{\mathrm{O}} \mathrm{G}_{\mathrm{O}}+\left(\Pi_{\mathrm{so}} /\left(1+\left(\theta_{\mathrm{O}}-1\right) \mathrm{M}_{\mathrm{O}}\right)\right) \theta_{\mathrm{S}} \mathrm{G}_{\mathrm{S}}+\sum \lambda_{\mathrm{oi}} x_{\mathrm{i}}  \tag{14}\\
& \lambda_{\mathrm{y}}=\lambda_{\mathrm{y} 0}+\sum \lambda_{\mathrm{yi}} x_{\mathrm{i}} \tag{15}
\end{align*}
$$

There are four $\Pi$ parameters that relate the minimum required levels of spending on social welfare and non-social welfare to the purchasing power of the income effects of the federal grants. The parameter $\Pi_{\mathrm{ij}}$ refers to the effect of a grant for the ith spending category on spending on the jth category of public goods. Because we have two categories of public goods, there are four parameters capturing "own" and "cross" effects of grants on public spending. The term in the denominators $\left(1+\left(\theta_{i}-1\right) \mathrm{M}_{\mathrm{i}}\right)$ is the price of spending on the ith public good. The term in the numerators $\theta_{i} G_{i}$ is the magnitude of the pure income effect of a federal grant aiding the ith public good. If the flypaper effect does not exist, all four $\Pi$ parameters are zero, and our model is identical to that expressed in equations (10), (11) and (12), with the parameters $\lambda_{\mathrm{s} 0}$ and $\lambda_{\mathrm{o} 0}$ taking the place of parameters $\lambda_{\mathrm{S}}$ and $\lambda_{\mathrm{O}}$, respectively. The $X$ variables are variables thought to affect governmental decision-makers' perceived need for public versus private spending (e.g., unemployment, poverty, etc.).

Substituting (13), (14) and (15) into (10), (11) and (12) gives a linear model with the flypaper parameters and need variables incorporated.
$L_{S}+G_{S}=a_{1}+b_{1} R_{L}+c_{1} G_{O}+d_{1} G_{S}+e_{1} M_{S}+f_{1} M_{O}+\sum g_{1 i} X_{i}+\sum h_{1 i} X_{i} M_{S}+\sum \varphi_{1 i} X_{i} M_{O}$
$\mathrm{L}_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2} \mathrm{R}_{\mathrm{L}}+\mathrm{c}_{2} \mathrm{G}_{\mathrm{O}}+\mathrm{d}_{2} \mathrm{G}_{\mathrm{S}}+\mathrm{e}_{2} \mathrm{M}_{\mathrm{S}}+\mathrm{f}_{2} \mathrm{M}_{\mathrm{O}}+\sum \mathrm{g}_{2 i} \mathrm{X}_{\mathrm{i}}+\sum \mathrm{h}_{2 \mathrm{i}} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{S}}+\sum \varphi_{2 \mathrm{i}} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{O}}$
$Y=a_{3}+b_{3} R_{L}+c_{3} G_{O}+d_{3} G_{s}+e_{3} M_{s}+f_{3} M_{o}+\sum g_{2 i} X_{i}+\sum h_{2 i} X_{i} M_{s}+\sum \varphi_{2 i} X_{i} M_{o}$
where

$$
\begin{aligned}
& a_{1}=\left(1-\beta_{\mathrm{S}}\right) \lambda_{\mathrm{s} 0}-\beta_{\mathrm{s}} \lambda_{\mathrm{o} 0}-\beta_{\mathrm{s}} \lambda_{\mathrm{y} 0} \\
& \mathrm{a}_{2}=-\beta_{\mathrm{o}} \lambda_{\mathrm{s} 0}+\left(1-\beta_{\mathrm{o}}\right) \lambda_{\mathrm{o} 0}-\beta_{\mathrm{o}} \lambda_{\mathrm{y} 0} \\
& \mathrm{a}_{3}=-\beta_{\mathrm{y}} \lambda_{\mathrm{s} 0}-\beta_{\mathrm{y}} \lambda_{\mathrm{o} 0}+\left(1-\beta_{\mathrm{y})} \lambda_{\mathrm{y} 0} \text { and } \mathrm{a}_{1}+\mathrm{a}_{2}+\mathrm{a}_{3}=0, \text { since } \beta_{\mathrm{s}}+\beta_{\mathrm{o}}+\beta_{\mathrm{y}}=1\right. \\
& \mathrm{b}_{1}=\beta_{\mathrm{s}} ; \mathrm{b}_{2}=\beta_{\mathrm{o}} ; \text { and } \mathrm{b}_{3}=\beta_{\mathrm{y}} ; \text { and } \mathrm{b}_{1}+\mathrm{b}_{2}+\mathrm{b}_{3}=1 \\
& \mathrm{c}_{1}=\theta_{\mathrm{o}}\left[\beta_{\mathrm{s}}+\left(1-\beta_{\mathrm{s}}\right) \Pi_{\mathrm{os}^{-}} \beta_{\mathrm{s}} \Pi_{\mathrm{oo}}\right]
\end{aligned}
$$

$$
\begin{aligned}
& c_{2}=\theta_{\mathrm{o}}\left[\beta_{\mathrm{o}}+\left(1-\beta_{\mathrm{o}}\right) \Pi_{\mathrm{oo}}-\beta_{\mathrm{o}} \Pi_{\mathrm{os}}\right] ; \\
& c_{3}=\theta_{0}\left[\beta_{y}-\beta_{y} \Pi_{o s^{-}} \beta_{y} \Pi_{\mathrm{oo}}\right] ; \quad \text { and } c_{1}+c_{2}+c_{3}=\theta_{\mathrm{o}} \\
& d_{1}=\theta_{\mathrm{s}}\left[\beta_{\mathrm{s}}+\left(1-\beta_{\mathrm{s}}\right) \Pi_{\mathrm{ss}}-\beta_{\mathrm{s}} \Pi_{\mathrm{so}}\right] \\
& d_{2}=\theta_{\mathrm{s}}\left[\beta_{\mathrm{o}}+\left(1-\beta_{\mathrm{o}}\right) \Pi_{\mathrm{so}}-\beta_{\mathrm{o}} \Pi_{\mathrm{SS}}\right] \\
& d_{3}=\theta_{s}\left[\beta_{y}-\beta_{y} \Pi_{s s}-\beta_{y} \Pi_{s o}\right] \text { and } d_{1}+d_{2}+d_{3}=\theta_{s} \\
& e_{1}=\lambda_{s 0}\left(1-\beta_{S}\right)\left(\theta_{\mathrm{S}}-1\right) ; e_{2}=-\lambda_{\mathrm{s} 0} \beta_{\mathrm{o}}\left(\theta_{\mathrm{S}}-1\right) ; \mathrm{e}_{3}=-\lambda_{\mathrm{s} 0} \beta_{\mathrm{y}}\left(\theta_{\mathrm{s}}-1\right) \text { and } \mathrm{e}_{1}+\mathrm{e}_{2}+\mathrm{e}_{3}=0 \\
& f_{1}=-\lambda_{\mathrm{o} 0} \beta_{\mathrm{s}}\left(\theta_{\mathrm{o}}-1\right) ; \mathrm{f}_{2}=\lambda_{\mathrm{o} 0}\left(1-\beta_{\mathrm{o}}\right)\left(\theta_{\mathrm{o}}-1\right) ; \mathrm{f}_{3}=-\lambda_{\mathrm{o} 0} \beta_{\mathrm{y}}\left(\theta_{\mathrm{o}}-1\right) \text { and } \mathrm{f}_{1}+\mathrm{f}_{2}+\mathrm{f}_{3}=0 \\
& \mathrm{~g}_{1 \mathrm{i}}=\left(1-\beta_{\mathrm{s}}\right) \lambda_{\mathrm{si}}-\beta_{\mathrm{s}} \lambda_{\mathrm{oi}}-\beta_{\mathrm{s}} \lambda_{\mathrm{yi}} ; \\
& \mathrm{g}_{2 \mathrm{i}}=-\beta_{\mathrm{o}} \lambda_{\mathrm{si}}+\left(1-\beta_{\mathrm{o}}\right) \lambda_{\mathrm{oi}}-\beta_{\mathrm{o}} \lambda_{\mathrm{yi}} \\
& g_{3 i}=-\beta_{y} \lambda_{s i}-\beta_{y} \lambda_{o i}+\left(1-\beta_{y} \lambda_{y i} \text { and } g_{1 i}+g_{2 i}+g_{3 i}=0\right. \\
& h_{1 i}=\lambda_{s i}\left(1-\beta_{S}\right)\left(\theta_{S}-1\right) ; h_{2 i}=-\lambda_{s i} \beta_{o}\left(\theta_{S}-1\right) ; h_{3 i}=-\lambda_{s i} \beta_{y}\left(\theta_{S}-1\right) \text { and } h_{1 i}+h_{2 i}+h_{3 i}=0 \\
& \varphi_{1 \mathrm{i}}=-\lambda_{\mathrm{oi}} \beta_{\mathrm{s}}\left(\theta_{\mathrm{O}}-1\right) ; \varphi_{2 \mathrm{i}}=\lambda_{\mathrm{oi}}\left(1-\beta_{\mathrm{o}}\right)\left(\theta_{\mathrm{O}}-1\right) ; \varphi_{3 \mathrm{i}}=-\lambda_{\mathrm{oi}} \beta_{\mathrm{y}}\left(\theta_{\mathrm{O}}-1\right) \text { and } \varphi_{1 \mathrm{i}}+\varphi_{2 \mathrm{i}}+\varphi_{3 \mathrm{i}}=0
\end{aligned}
$$

Within this framework, we can estimate a series of models that incorporate various constraints. We report the model results for the four public good model, which is a generalization of the two good model summarized above. ${ }^{6}$ For this model we will report results for the following special and general cases:
${ }^{6}$ The model structure in equations (16) and (17) can be generalized for four public goods to become four equations of the general form::
$L_{i}+G_{i}=a_{i}+b_{i} R_{L}+\sum \delta_{j} G_{j}+\sum \lambda_{j} M_{j}+\sum \sum \xi_{j k} X_{k} M_{j}$ where $j=1, \ldots, 4$; and $k=1, \ldots$ n and $n$ is the number of "need" variables in the equation. Equation (18) becomes:
$Y==a_{5}+b_{5} R_{L}+\sum \delta_{j} G_{j}+\sum \lambda_{j} M_{j}+\sum \sum \xi_{j k} X_{k} M_{j}$ with similar constraints applying to the system. We need only estimate the first four equations because the coefficients in the income equation are linear combinations of the coefficients in the first four equations.
In order to estimate the four public good model from the Census data, it was necessary to deal with a major problem posed by data limitations. McGuire's approach assumes that we have the same level of detail for spending as for intergovernmental grants. Unfortunately, we do not for social welfare spending. The intergovernmental revenue variable used to measure federal grants is available only for the broad aggregates of social welfare spending and non-social welfare spending, while social welfare spending is available for three subcategories of spending; cash assistance, Medicaid, and other social welfare. Therefore, to estimate Models 2 and 3, we needed to assume that the ratio of federal grants for a

- Model 1A: A model with no price effects (all $\theta=1$ ), no flypaper effects (all $\Pi=0$ ), and without "need" variables (all $\lambda_{\mathrm{ji}}=0$ );
- Model 1B: A model with no price effects (all $\theta=1$ ), no flypaper effects (all $\Pi_{\mathrm{OS}}=0$ ), but including need variables;
- Model 1C: A model with no price effects (all $\theta=1$ ), no need variables, but including flypaper effects; and
- Model 1D: A model with no price effects, including need variables and including flypaper effects.
- Model 2A: A model with no income effects of grants (all $\theta=0$ ) (as a consequence, flypaper effects do not exist), and without need variables (all $\lambda_{\mathrm{ji}}=0$ );
- Model 2B: A model with no income effects of grants (all $\theta=0$ ) (as a consequence, flypaper effects do not exist), and including need variables.
- Model 3A: A model with estimated price effects, no flypaper effects (all $\Pi=0$ ), and without "need" variables;
- Model 3B: A model with estimated price effects, including need variables and including flypaper effects.

We estimated each of these models using annual data over the time period 1978 to 2001 for all states, and also separately for four quartiles of states based on average state per capita personal income over the observation period.

## Model 1A Specification

Model 1A is the simplest, but least realistic model. It assumes that the grantee government responds to all grants as though they were unconditional, and that grant income affects public spending levels and allocations in the same way as income in the private sector. It also assumes that a state's "needs" are adequately represented by linear state effects (i.e., allowing the constant term in the regression to be different for each state). The latter assumption would be consistent with unbiased estimates of regression coefficients only if needs were uncorrelated with included independent variables (fiscal capacity and grant levels).

The model reduces to:
$L_{S}+G_{S}=a_{1}+b_{1} R_{L}+c_{1} G_{O}+d_{1} G_{S}\left(\right.$ with $\left.b_{1}=c_{1}=d_{1}=\beta_{S}\right)$ or $L_{S}+G_{S}=a_{1}+b_{1}\left(R_{L}+G_{O}+G_{S}\right)$
subcategory of social welfare to total grants for social welfare was constant. This enabled us to replace $M_{j}$ by $\left[G^{S W} /\left(S_{j}+G_{j}\right)\right]$ which on that assumption is linearly related to $M_{j}=G_{j} /\left(S_{j}+G_{j}\right)$. Since $S_{j}+G_{j}$ is observed, although $\mathrm{G}_{\mathrm{j}}$ is not, we can estimate the four good model.
$L_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2} \mathrm{R}_{\mathrm{L}}+\mathrm{c}_{2} \mathrm{G}_{\mathrm{O}}+\mathrm{d}_{2} \mathrm{G}_{\mathrm{S}}\left(\right.$ with $\left.\mathrm{b}_{2}=\mathrm{c}_{2}=\mathrm{d}_{2}=\beta_{\mathrm{o}}\right)$ or $\mathrm{L}_{\mathrm{S}}+\mathrm{G}_{\mathrm{S}}=\mathrm{a}_{2}+\mathrm{b}_{2}\left(\mathrm{R}_{\mathrm{L}}+\mathrm{G}_{\mathrm{O}}+\mathrm{G}_{\mathrm{S}}\right)$
$Y=a_{3}+b_{3} R_{L}+c_{3} G_{O}+d_{3} G_{S}\left(\right.$ with $\left.b_{3}=c_{3}=d_{3}=\beta_{y}\right)$ or $Y=a_{3}+b_{3}\left(R_{L}+G_{O}+G_{S}\right)$
The regression results are shown in Exhibit A-1.
Exhibit A-1
SWS Model 1A Coefficient Estimates With Year Dummies


CA means Cash Assistance, M means Medicaid, OW means Non-health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending.

## Model 1B Specification

Model 1B improves on Model 1A by introducing objective measures of need thought to affect the minimum required spending levels in each state. However, like Model 1A, this model also assumes that governmental decision-makers respond to grant income in the same way as private income, and that all grant income is unconditional.
$\mathrm{L}_{\mathrm{S}}+\mathrm{G}_{\mathrm{S}}=\mathrm{a}_{1}+\mathrm{b}_{1}\left(\mathrm{R}_{\mathrm{L}}+\mathrm{G}_{\mathrm{O}}+\mathrm{G}_{\mathrm{S}}\right)+\sum \mathrm{g}_{1 \mathrm{i}} \mathrm{X}_{\mathrm{i}}$
$\mathrm{L}_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2}\left(\mathrm{R}_{\mathrm{L}}+\mathrm{G}_{\mathrm{O}}+\mathrm{G}_{\mathrm{S}}\right)+\sum \mathrm{g}_{2 \mathrm{i}} \mathrm{X}_{\mathrm{i}}$
$Y=a_{3}+b_{3}\left(R_{L}+G_{O}+G_{S}\right)+\sum g_{3 i} X_{i}$
The regression results for Model 1B are reported in Exhibit A-2.
SWS Model 1B Coefficient Estimates With Year Dummies

| Variable |  |  | Adjusted <br> R-Squared | Constant |  | Federal grants |  | Population Density |  | Unemployment per capita |  | Poverty per capita (mov. avg) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Overall |  | CA | 0.86 | 120.13 | (6.63) | 0.00 | (7.03) | 0.03 | (3.56) | 893.64 | (7.43) | -13.79 | (0.46) |
|  |  | M | 0.86 | 85.51 | (3.39) | 0.00 | (3.00) | -0.17 | (14.12) | 823.77 | (4.92) | -51.51 | (1.24) |
|  |  | OW | 0.86 | -9.13 | (0.41) | 0.01 | (8.95) | -0.06 | (5.98) | 13.89 | (0.09) | -31.89 | (0.87) |
|  |  | PH | 0.88 | 235.51 | (13.14) | 0.00 | (0.61) | -0.07 | (8.40) | 307.77 | (2.58) | -52.79 | (1.80) |
|  |  | NSWS | 0.96 | 2082.94 | (8.12) | 0.12 | (14.95) | 0.54 | (4.52) | 7753.83 | (4.55) | 235.55 | (0.56) |
| Quartile | 1 | CA | 0.88 | 348.46 | (9.97) | -0.01 | (7.46) | 0.02 | (2.16) | 1268.17 | (4.34) | 1.03 | (0.02) |
|  |  | M | 0.89 | 278.07 | (5.50) | 0.00 | (2.36) | -0.16 | (10.84) | 1806.93 | (4.27) | -79.20 | (1.17) |
|  |  | OW | 0.86 | 110.66 | (2.38) | 0.01 | (5.58) | -0.06 | (4.62) | 436.27 | (1.12) | -47.49 | -(0.76) |
|  |  | PH | 0.86 | 84.32 | (2.58) | 0.00 | (4.03) | -0.07 | (7.03) | 33.30 | (0.12) | -5.30 | (0.12) |
|  |  | NSWS | 0.95 | 422.63 | (0.58) | 0.13 | (7.03) | 0.60 | (2.82) | 13011.00 | (2.15) | 1069.61 | (1.11) |
|  | 2 | CA | 0.74 | -264.37 | (3.65) | 0.01 | (2.94) | 0.41 | (3.60) | 1290.72 | (4.37) | 536.67 | (3.82) |
|  |  | M | 0.85 | 123.48 | (1.76) | 0.00 | (0.02) | 0.03 | (0.23) | 115.43 | (0.40) | 265.27 | (1.95) |
|  |  | OW | 0.87 | -97.11 | (1.36) | 0.01 | (4.36) | -0.30 | (2.66) | 92.95 | (0.32) | 67.09 | (0.49) |
|  |  | PH | 0.90 | 394.37 | (7.55) | -0.01 | (3.44) | -0.28 | (3.41) | 608.31 | (2.85) | 63.69 | (0.63) |
|  |  | NSWS | 0.94 | 3635.61 | (5.86) | 0.06 | (3.22) | 2.48 | (2.56) | 11168.00 | (4.41) | 689.43 | (0.57) |

Exhibit A-2 (continued)
SWS Model 1B Coefficient Estimates Wit

| Variable |  |  | Adjusted <br> R-Squared | Constant |  | Federal grants |  | Population Density |  | Unemployment per capita |  | Poverty per capita (mov. <br> avg) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Quartile | 3 | CA | 0.82 | -67.97 | (2.14) | 0.00 | (2.37) | 0.92 | (6.47) | 464.71 | (2.89) | 178.59 | (3.24) |
|  |  | M | 0.84 | -32.05 | (0.49) | 0.01 | (3.62) | -0.01 | (0.03) | 575.61 | (1.74) | 117.18 | (1.03) |
|  |  | OW | 0.83 | 229.28 | (3.48) | 0.01 | (2.62) | -2.31 | (7.83) | 494.09 | (1.48) | -252.43 | (2.21) |
|  |  | PH | 0.88 | -9.44 | (0.16) | 0.00 | (0.30) | 0.10 | (0.37) | -337.02 | (1.15) | -59.03 | (0.59) |
|  |  | NSWS | 0.96 | 2405.27 | (6.84) | 0.08 | (5.88) | -0.48 | (0.31) | 6510.21 | (3.65) | -2212.71 | (3.62) |
|  | 4 | CA | 0.36 | 59.35 | (1.17) | 0.00 | (2.22) | 1.09 | (3.30) | 176.84 | (0.76) | 68.31 | (1.16) |
|  |  | M | 0.81 | -46.44 | (0.47) | 0.01 | (2.61) | 0.04 | (0.06) | -442.19 | (0.99) | 422.12 | (3.73) |
|  |  | OW | 0.79 | 76.57 | (1.49) | 0.00 | (1.82) | -0.31 | (0.92) | -339.21 | (1.45) | 26.31 | (0.44) |
|  |  | PH | 0.95 | -224.76 | (4.80) | 0.00 | (0.99) | 2.97 | (9.80) | 283.29 | (1.33) | 93.61 | (1.73) |
|  |  | NSWS | 0.95 | 2063.04 | (4.23) | 0.02 | (0.85) | 15.29 | (4.84) | -4887.97 | (2.19) | 157.56 | (0.28) |
| CA means Cash Assistance, M means Medicaid, OW means Non-health Social Services, PH means Public Hospital Spending, and NSWS Welfare Spending. |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Model 1C Specification

Model 1C is our first attempt to incorporate so-called "flypaper" effects. We still have only income effects without incorporating the price effects of grants, but we allow the effect on federal grants on spending allocation to be different depending on the source of the income. In particular, it is believed that, quite aside from price effects, federal grants have a stronger effect on public spending than on private spending. Model 1C omits need variables. The model can be written as:
$L_{S}+G_{S}=a_{1}+b_{1}\left(R_{L}+G_{O}+G_{S}\right)+\left(c_{1}-b_{1}\right) G_{O}+\left(d_{1}-b_{1}\right) G_{S}$ with $c_{1}-b_{1}>0, d_{1}-b_{1}>0$
$L_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2}\left(\mathrm{R}_{\mathrm{L}}+\mathrm{G}_{\mathrm{O}}+\mathrm{G}_{\mathrm{S}}\right)+\left(\mathrm{c}_{2}-\mathrm{b}_{2}\right) \mathrm{G}_{\mathrm{O}}+\left(\mathrm{d}_{2}-\mathrm{b}_{2}\right) \mathrm{G}_{\mathrm{S}}$ with $\mathrm{c}_{2}-\mathrm{b}_{2}>0, \mathrm{~d}_{2}-\mathrm{b}_{2}>0$
$\mathrm{Y}=\mathrm{a}_{3}+\mathrm{b}_{3}\left(\mathrm{R}_{\mathrm{L}}+\mathrm{G}_{\mathrm{O}}+\mathrm{G}_{\mathrm{S}}\right)+\left(\mathrm{c}_{3}-\mathrm{b}_{3}\right) \mathrm{G}_{\mathrm{O}}+\left(\mathrm{d}_{3}-\mathrm{b}_{3}\right) \mathrm{G}_{\mathrm{S}}$ with $\mathrm{c}_{3}-\mathrm{b}_{3}<0, \mathrm{~d}_{3}-\mathrm{b}_{3}<0$
The regression results are reported in Exhibit A-3.
Appendix A: Theoretical Foundations


| Variable |  |  | Adjusted RSquared | Constant |  | Per capita personal income |  | Federal grants for nonsocial welfare |  | Federal grants for social welfare |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Quartile | 3 | CA | 0.81 | -56.20 | (1.89) | 0.00 | (2.50) | -0.01 | (0.67) | 0.14 | (7.70) |
|  |  | M | 0.89 | -139.61 | (2.84) | 0.00 | (3.02) | 0.01 | (0.30) | 0.34 | (11.48) |
|  |  | NSS | 0.84 | -80.35 | (1.38) | 0.00 | (1.19) | 0.23 | (8.34) | 0.16 | (4.55) |
|  |  | PH | 0.89 | -137.54 | (2.70) | 0.00 | (1.13) | 0.02 | (0.89) | 0.12 | (3.77) |
|  |  | NSWS | 0.96 | 1664.78 | (5.13) | 0.09 | (9.18) | 0.55 | (3.52) | 0.04 | (0.19) |
|  | 4 | CA | 0.34 | 155.28 | (3.57) | 0.00 | (1.65) | -0.04 | (1.98) | -0.02 | (1.30) |
|  |  | M | 0.89 | -136.14 | (2.24) | 0.01 | (2.90) | 0.03 | (1.04) | 0.34 | (15.43) |
|  |  | NSS | 0.79 | 93.09 | (2.18) | 0.00 | (1.91) | -0.01 | (0.66) | -0.04 | (2.42) |
|  |  | PH | 0.94 | -93.39 | (2.04) | 0.01 | (4.56) | -0.06 | (2.41) | 0.03 | (2.08) |
|  |  | NSWS | 0.94 | 1890.66 | (4.43) | 0.06 | (3.45) | 0.54 | (2.48) | 0.16 | (1.03) |
| CA means Cash Assistance, M means Medicaid, NSS means Non-health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending. |  |  |  |  |  |  |  |  |  |  |  |

## Model 1D Specification

Model 1D adds need variables to the structure in Model 1C.

$$
\begin{aligned}
& L_{\mathrm{S}}+\mathrm{G}_{\mathrm{S}}=\mathrm{a}_{1}+\mathrm{b}_{1}\left(\mathrm{R}_{\mathrm{L}}+\mathrm{G}_{\mathrm{O}}+\mathrm{G}_{\mathrm{S}}\right)+\left(\mathrm{c}_{1}-\mathrm{b}_{1}\right) \mathrm{G}_{\mathrm{O}}+\left(\mathrm{d}_{1}-\mathrm{b}_{1}\right) \mathrm{G}_{\mathrm{S}}+\sum \mathrm{g}_{1 \mathrm{i}} x_{\mathrm{i}} \\
& \mathrm{~L}_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2}\left(\mathrm{R}_{\mathrm{L}}+\mathrm{G}_{\mathrm{O}}+\mathrm{G}_{\mathrm{S}}\right)+\left(\mathrm{c}_{2}-\mathrm{b}_{2}\right) \mathrm{G}_{\mathrm{O}}+\left(\mathrm{d}_{2}-\mathrm{b}_{2}\right) \mathrm{G}_{\mathrm{S}}+\sum \mathrm{g}_{2 \mathrm{i}} x_{\mathrm{i}} \\
& \mathrm{Y}=\mathrm{a}_{3}+\mathrm{b}_{3}\left(\mathrm{R}_{\mathrm{L}}+\mathrm{G}_{\mathrm{O}}+\mathrm{G}_{\mathrm{S}}\right)+\left(\mathrm{c}_{3}-\mathrm{b}_{3}\right) \mathrm{G}_{\mathrm{O}}+\left(\mathrm{d}_{3}-\mathrm{b}_{3}\right) \mathrm{G}_{\mathrm{S}}+\sum \mathrm{g}_{3 i} x_{\mathrm{i}}
\end{aligned}
$$

The regression results are reported in Exhibit A-4.
Appendix A: Theoretical Foundations
SWS Model 1D Coefficient Estimates With Year Dummies

Appendix A: Theoretical Foundations

| Quartile |  | riable | Adjusted <br> R- <br> Squared | Constant |  | Per capita personal income |  | Federal grants for nonsocial welfare |  | Federal grants for social welfare |  | Population Density |  | Unemployment per capita |  | Poverty per capita (mov. avg) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3 | M | 0.89 | -202.85 | (3.42) | 0.005 | (2.54) | 0.02 | (0.66) | 0.35 | (11.65) | 0.35 | (1.36) | 451.51 | (1.64) | 84.89 | (0.91) |
|  |  | NSS | 0.86 | 25.85 | (0.39) | 0.005 | (2.09) | 0.18 | (6.75) | 0.14 | (4.22) | -1.59 | (5.54) | 196.59 | (0.64) | -258.74 | (2.47) |
|  |  | PH | 0.89 | -91.59 | (1.48) | -0.001 | (0.33) | 0.03 | (1.21) | 0.12 | (3.88) | 0.32 | (1.18) | -420.39 | (1.46) | -69.47 | (0.71) |
|  |  | NSWS | 0.96 | 2099.03 | (5.48) | 0.080 | (5.86) | 0.50 | (3.19) | 0.03 | (0.16) | 0.88 | (0.53) | 5923.35 | (3.32) | -2192.36 | (3.62) |
|  | 4 | CA | 0.37 | 77.23 | (1.49) | -0.004 | (1.88) | -0.03 | (1.53) | -0.03 | (1.70) | 1.01 | (3.04) | 139.93 | (0.59) | 94.24 | (1.51) |
|  |  | M | 0.89 | -164.18 | (2.22) | 0.008 | (2.62) | 0.03 | (0.99) | 0.34 | (14.77) | -0.04 | (0.07) | 382.24 | (1.14) | -4.42 | (0.05) |
|  |  | NSS | 0.80 | 100.31 | (1.95) | 0.005 | (2.14) | -0.02 | (0.70) | -0.05 | (2.85) | -0.34 | (1.03) | -452.51 | (1.93) | 89.02 | (1.43) |
|  |  | PH | 0.95 | -221.98 | (4.69) | 0.002 | (1.18) | -0.03 | (1.50) | 0.03 | (1.89) | 2.87 | (9.39) | 372.15 | (1.73) | 56.02 | (0.98) |
|  |  | NSWS | 0.95 | 1797.11 | (3.68) | 0.005 | (0.23) | 0.71 | (3.40) | 0.08 | (0.50) | 17.17 | (5.45) | -5225.86 | (2.35) | 162.03 | (0.28) |

## Model 2A Specification

The Model 2 series of models is based on the assumption that grants have price effects but no income effects (i.e.,. This is at the other extreme from the Model 1 series of models which assumed that grants have only income effects but no price effects. The type of grant envisioned in the Model 1 series is an unconditional, non-matching grant, e.g., revenue sharing. The type of grant envisioned in the Model 2 series is a block grant restricted to the aided activity with maintenance of effort requirements. Model 2A has no income effects $\left(\theta_{\mathrm{O}}=\theta_{\mathrm{S}}=0\right)$ and has no need variables ( $\lambda_{\mathrm{si}}=\lambda_{\mathrm{oi}}=\lambda_{\mathrm{yi}}=0$ ).
$L_{S}+G_{S}=a_{1}+b_{1} R_{L}+e_{1} M_{S}+f_{1} M_{o}$
$\mathrm{L}_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2} \mathrm{R}_{\mathrm{L}}+\mathrm{e}_{2} \mathrm{M}_{\mathrm{s}}+\mathrm{f}_{2} \mathrm{M}_{\mathrm{O}}$
$Y=a_{3}+b_{3} R_{L}+e_{3} M_{S}+f_{3} M_{O}$
The Model 2A estimates are reported in Exhibit A-5.

| Variable |  |  | Adjusted R- <br> Squared | Constant |  | Per capita total income |  | Ratio of federal social welfare grants to cash assistance spending |  | Ratio of federal social welfare grants to payment to medical vendors |  | Ratio of federal social welfare grants to other welfare |  | Ratio of federal <br> non-social welfare grants to state-local spending on nonsocial welfare |  | Ratio of federal non-socia welfare grants to public hospital spending |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Overall |  | CA | 0.87 | 134.47 | (6.72) | 0.00 | (8.41) | -0.76 | (8.06) | -2.70 | (1.55) | 6.88 | (7.75) | 63.67 | (1.92) | 0.00 | (0.25) |
|  |  | M | 0.89 | 93.89 | (3.71) | 0.00 | (5.75) | 0.26 | (2.22) | -38.26 | (17.41) | 17.88 | (15.93) | -200.83 | (4.78) | 0.00 | (2.19) |
|  |  | NSS | 0.90 | 134.55 | (6.36) | 0.00 | (5.88) | 0.17 | (1.68) | 2.65 | (1.44) | -21.01 | (22.38) | -49.64 | (1.41) | 0.00 | (6.13) |
|  |  | PH | 0.88 | 192.01 | (9.48) | 0.00 | (2.63) | 0.40 | (4.24) | 3.43 | (1.95) | 7.09 | (7.90) | -83.95 | (2.50) | 0.00 | (1.33) |
|  |  | NSWS | 0.96 | 4173.92 | (14.38) | 0.09 | (11.01) | 0.52 | (0.38) | -11.65 | (0.46) | -41.60 | (3.23) | -3378.27 | (7.02) | 0.01 | (1.39) |
| Quartile | 1 | CA | 0.90 | 328.48 | (10.41) | -0.01 | (7.20) | -4.19 | (4.18) | 1.95 | (0.40) | 15.91 | (6.02) | 259.73 | (3.88) | -0.43 | (0.46) |
|  |  | M | 0.89 | 153.83 | (3.04) | 0.01 | (5.00) | -2.37 | (1.47) | -66.22 | (8.49) | 31.08 | (7.32) | -117.89 | (1.10) | -4.81 | (3.18) |
|  |  | NSS | 0.90 | 260.96 | (6.60) | 0.01 | (4.98) | 0.67 | (0.53) | -11.35 | (1.86) | -35.34 | (10.66) | -33.55 | (0.40) | -6.23 | (5.28) |
|  |  | PH | 0.90 | 2.79 | (0.10) | 0.01 | (7.64) | -0.71 | (0.80) | -8.25 | (1.93) | 2.09 | (0.90) | 292.87 | (4.96) | -10.83 | (13.05) |
|  |  | NSWS | 0.95 | 2700.88 | (3.72) | 0.11 | (5.60) | 9.12 | (0.40) | -152.61 | (1.37) | $161.24$ | (2.65) | -1717.99 | (1.12) | -43.45 | (2.01) |
|  | 2 | CA | 0.73 | -10.73 | (0.14) | 0.00 | (0.65) | -1.53 | (4.93) | -7.07 | (0.91) | 12.53 | (3.71) | 23.80 | (0.22) | -4.13 | (1.62) |
|  |  | M | 0.94 | 233.76 | (5.31) | 0.00 | (0.22) | -0.36 | (2.01) | -68.47 | (15.20) | 21.61 | (10.97) | -107.92 | (1.72) | -3.14 | (2.12) |
|  |  | NSS | 0.91 | 209.33 | (3.53) | 0.00 | (0.49) | -0.36 | (1.48) | 7.60 | (1.25) | -27.09 | (10.20) | 11.95 | (0.14) | 5.33 | (2.66) |
|  |  | PH | 0.95 | 447.03 | (11.88) | -0.01 | (5.84) | 0.31 | (1.98) | -5.10 | (1.32) | 3.76 | (2.23) | 11.03 | (0.21) | -18.28 | (14.38) |
|  |  | NSWS | 0.96 | 9129.76 | (17.84) | -0.05 | (3.78) | -2.90 | (1.38) | -24.80 | (0.47) | 10.35 | (0.45) | -9282.76 | (12.72) | 108.10 | (6.25) |

Exhibit A-5 (continued)
SWS Model 2A Coefficient Estimates With Year Dummies

| Quartile | 3 | Variable | Adjusted RSquared | Constant |  | Per capita total income |  | Ratio of federal social welfare grants to cash assistance spending |  | Ratio of federal <br> social <br> welfare grants to payment to medical vendors |  | Ratio of federal social welfare grants to other welfare |  |  |  | Ratio of federal non-social welfare grants to public hospital spending |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | M | 0.89 | 200.69 | (3.93) | 0.00 | (1.86) | -0.35 | (1.85) | -24.33 | (11.36) | 3.60 | (2.16) | -113.51 | (1.42) | 0.00 | (1.90) |
|  |  | NSS | 0.91 | 228.21 | (4.87) | 0.00 | (0.60) | 0.14 | (0.82) | 1.68 | (0.86) | -22.74 | (14.83) | 367.15 | (5.01) | 0.00 | (5.34) |
|  |  | PH | 0.89 | -146.32 | (2.76) | 0.00 | (2.28) | 0.06 | (0.29) | 9.51 | (4.27) | 5.09 | (2.93) | 103.12 | (1.24) | 0.00 | (1.60) |
|  |  | NSWS | 0.96 | 3118.14 | (9.20) | 0.07 | (5.79) | 1.49 | (1.20) | -12.62 | (0.89) | -13.91 | (1.25) | -2198.79 | (4.15) | 0.01 | (2.58) |
|  |  | CA | 0.51 | 128.56 | (3.45) | 0.00 | (1.35) | -0.69 | (8.11) | -5.08 | (1.23) | 4.66 | (4.96) | -179.56 | (2.72) | -0.26 | (0.16) |
|  |  | M | 0.92 | 121.34 | (2.25) | 0.01 | (2.16) | 0.53 | (4.26) | -75.42 | (12.60) | 19.46 | (14.28) | -4.66 | (0.05) | 0.12 | (0.05) |
|  | 4 | NSS | 0.91 | 185.22 | (6.50) | 0.00 | (0.49) | 0.10 | (1.48) | 8.34 | (2.64) | -12.80 | (17.78) | -103.67 | (2.05) | 1.30 | (1.05) |
|  |  | PH | 0.96 | -142.22 | (3.93) | 0.01 | (6.40) | 0.23 | (2.81) | 5.04 | (1.25) | 4.31 | (4.71) | 282.63 | (4.40) | -18.27 | (11.59) |
|  |  | NSWS | 0.95 | 2949.56 | (7.12) | 0.05 | (2.97) | 0.38 | (0.41) | -81.94 | (1.78) | -1.66 | (0.16) | -3233.69 | (4.40) | 31.09 | (1.73) |

## Model 2B Specification

Model 2B is the same as model 2A except that Model 2B includes need variables and their interactions.

$$
\begin{aligned}
& L_{\mathrm{S}}+\mathrm{G}_{\mathrm{S}}=\mathrm{a}_{1}+\mathrm{b}_{1} \mathrm{R}_{\mathrm{L}}+\mathrm{e}_{1} \mathrm{M}_{\mathrm{S}}+\mathrm{f}_{1} \mathrm{M}_{\mathrm{O}}+\sum \mathrm{g}_{1 \mathrm{i}} \mathrm{X}_{\mathrm{i}}+\sum \mathrm{h}_{1 \mathrm{i}} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{S}}+\sum \varphi_{1 \mathrm{i}} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{O}} \\
& \mathrm{~L}_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2} \mathrm{R}_{\mathrm{L}}+\mathrm{e}_{2} \mathrm{M}_{\mathrm{S}}+\mathrm{f}_{2} \mathrm{M}_{\mathrm{O}}+\sum \mathrm{g}_{2 i} \mathrm{X}_{\mathrm{i}}+\sum \mathrm{h}_{2 \mathrm{i}} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{S}}+\sum \varphi_{2 \mathrm{i}} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{O}} \\
& \mathrm{Y}=\mathrm{a}_{3}+\mathrm{b}_{3} \mathrm{R}_{\mathrm{L}}+\mathrm{e}_{3} \mathrm{M}_{\mathrm{S}}+\mathrm{f}_{3} \mathrm{M}_{\mathrm{O}}+\sum \mathrm{g}_{3 i} \mathrm{X}_{\mathrm{i}}+\sum \mathrm{h}_{3 i} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{S}}+\sum \varphi_{3 i} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{O}}
\end{aligned}
$$

The estimates are reported in Exhibit A-6.

Exhibit A-6
SWS Model 2B Coefficient Estimates With Year Dummies

| Variable | Overall |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | CA | M | NSS | PH | NSWS |
| Adjusted R-Squared | 0.89 | 0.92 | 0.92 | 0.91 | 0.96 |
| Constant | 52.01 | 49.52 | 139.18 | 130.98 | 4539.82 |
|  | (1.99) | (1.66) | (4.93) | (5.13) | (11.95) |
| Per capita total income | 0.00 | 0.00 | 0.00 | 0.00 | 0.10 |
|  | (3.44) | (3.05) | (3.12) | (2.94) | (10.94) |
| Ratio of federal social welfare grants to cash assistance spending | 1.45 | -1.54 | -0.55 | 0.25 | 2.20 |
|  | (3.90) | (3.61) | (1.37) | (0.70) | (0.41) |
| Ratio of federal social welfare grants to payment to medical vendors | -10.85 | 8.50 | -10.51 | 14.06 | -1.90 |
|  | (1.50) | (1.03) | (1.34) | (1.99) | (0.02) |
| Ratio of federal social welfare grants to other welfare | 7.93 | 15.54 | -21.27 | 5.76 | -18.55 |
|  | (8.93) | (15.29) | (22.16) | (6.63) | (1.44) |
| Ratio of federal non-social welfare grants to statelocal spending on non-social welfare | 142.83 | -31.21 | 312.56 | 54.97 | -7658.06 |
|  | (1.74) | (0.33) | (3.52) | (0.68) | (6.42) |
| Ratio of federal non-social welfare grants to public hospital spending | 0.55 | 1.76 | -0.27 | 1.58 | -12.63 |
|  | (0.98) | (2.76) | (0.44) | (2.90) | (1.56) |
| Population Density | -0.05 | -0.11 | -0.05 | 0.02 | 1.61 |
|  | (2.21) | (4.43) | (2.09) | (1.08) | (5.14) |
| Unemployment per capita | 2021.09 | 1603.20 | 955.22 | -455.08 | 32077.00 |
|  | (6.37) | (4.42) | (2.78) | (1.47) | (6.95) |
| Poverty per capita (mov. avg) | -79.48 | 128.86 | -150.50 | 388.10 | -8019.02 |
|  | (0.80) | (1.14) | (1.41) | (4.01) | (5.57) |
| Interaction (Mo*Population Density) | 0.03 | 0.01 | 0.05 | 0.06 | 0.05 |
|  | (2.78) | (0.70) | (3.52) | (4.75) | (0.31) |
| Interaction (Mo*Unemployment per capita) | -4273.21 | -6548.46 | -10610.00 | 8576.81 | -175022.00 |
|  | (2.26) | (3.03) | (5.20) | (4.65) | (6.38) |
| Interaction (Mo*Poverty per capita (mov. avg.)) | -220.95 | 1693.39 | 130.59 | -2128.83 | 59210.00 |
|  | (0.41) | (2.75) | (0.22) | (4.04) | (7.55) |
| Interaction (Ms1*Population Density) | 0.00 | 0.00 | 0.00 | 0.00 | -0.01 |
|  | (0.48) | (4.10) | (3.47) | (8.79) | (1.88) |
| Interaction (Ms1*Unemployment per capita) | -109.24 | -13.70 | 117.32 | -182.84 | 268.92 |
|  | (4.23) | (0.46) | (4.20) | (7.24) | (0.72) |

## Exhibit A-6 (continued) <br> SWS Model 2B Coefficient Estimates With Year Dummies

| Variable | Overall |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | CA | M | NSS | PH | NSWS |
| Interaction (Ms1*Poverty per capita (mov. avg.)) | 10.22 | -11.18 | -13.22 | 12.38 | 57.99 |
|  | (2.82) | (2.70) | (3.38) | (3.50) | (1.10) |
| Interaction (Ms2*Population Density) | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
|  | (0.57) | (3.80) | (0.44) | (1.11) | (0.16) |
| Interaction (Ms2*Unemployment per capita) | -174.91 | 56.81 | 35.30 | 10.23 | -585.01 |
|  | (9.21) | (2.61) | (1.72) | (0.55) | (2.12) |
| Interaction (Ms2*Poverty per capita (mov. avg.)) | 12.41 | 3.48 | -0.93 | 0.00 | 91.70 |
|  | (4.33) | (1.06) | (0.30) | (0.00) | (2.20) |
| Interaction (Ms3*Population Density) | 0.01 | -0.02 | -0.01 | 0.00 | 0.01 |
|  | (3.34) | (5.19) | (1.84) | (1.14) | (0.23) |
| Interaction (Ms3*Unemployment per capita) | 284.82 | -255.37 | -52.51 | 132.03 | 1464.63 |
|  | (1.78) | (1.39) | (0.30) | (0.84) | (0.63) |
| Interaction (Ms3*Poverty per capita (mov. avg.)) | -13.26 | -318.68 | 137.30 | -130.57 | -339.38 |
|  | (0.23) | (4.90) | (2.24) | (2.35) | (0.41) |

CA means Cash Assistance, M means Medicaid, NSS means Non-Health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending.

## Exhibit A-6(1)

SWS Model 2B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 |  |  |  |  | 2 |  |  |  |  |
|  |  | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Adjusted R-Squared | 0.92 | 0.95 | 0.92 | 0.94 | 0.97 | 0.87 | 0.96 | 0.93 | 0.98 | 0.97 |
| Constant | 245.36 | 297.06 | 267.43 | -66.79 | 581.60 | -272.52 | -1.78 | 68.51 | 275.08 | 7669.99 |
|  | (5.23) | (5.16) | (4.68) | (1.86) | (0.62) | (3.98) | (0.04) | (0.99) | (7.86) | (13.67) |
| Per capita total income | 0.00 | 0.01 | 0.00 | 0.01 | 0.19 | 0.01 | 0.00 | 0.01 | 0.00 | 0.02 |
|  | (4.30) | (4.11) | (3.77) | (8.67) | (9.41) | (3.32) | (2.78) | (3.23) | (0.29) | (0.94) |
| Ratio of federal social welfare grants to cash assistance spending | 9.52 | -27.91 | -4.69 | 7.06 | 27.10 | 1.28 | -0.83 | -3.51 | -0.56 | -25.37 |
|  | (2.60) | (6.20) | (1.05) | (2.52) | (0.37) | (0.70) | (0.62) | (1.90) | (0.61) | (1.70) |
| Ratio of federal social welfare grants to payment to medical vendors | -32.99 | -88.02 | -39.98 | -58.58 | -571.13 | 20.07 | -4.92 | 27.58 | 19.69 | 392.17 |
|  | (1.68) | (3.64) | (1.67) | (3.89) | (1.44) | (0.79) | (0.26) | (1.06) | (1.51) | (1.87) |
| Ratio of federal social welfare grants to other welfare | 13.29 | 25.74 | -33.11 | 0.04 | -108.88 | 15.36 | 19.86 | -29.60 | 1.04 | -2.88 |
|  | (5.11) | (8.05) | (10.44) | (0.02) | (2.08) | (5.98) | (10.54) | (11.35) | (0.79) | (0.14) |

## Exhibit A-6(1) (continued) SWS Model 2B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 |  |  |  |  | 2 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Ratio of federal nonsocial welfare grants to state-local spending on non-social welfare | 308.45 | 492.39 | 741.77 | 824.92 | 7780.91 | -354.41 | -80.79 | -679.99 | -656.14 | -20616.00 |
|  | (1.83) | (2.38) | (3.62) | (6.41) | (2.30) | (1.39) | (0.43) | (2.63) | (5.04) | (9.88) |
| Ratio of federal nonsocial welfare grants to public hospital spending | 4.43 | 4.67 | -8.69 | -7.60 | -433.83 | 23.20 | -9.50 | 32.16 | -3.92 | 225.31 |
|  | (1.37) | (1.18) | (2.21) | (3.08) | (6.67) | (1.97) | (1.10) | (2.69) | (0.65) | (2.33) |
| Population Density | -0.04 | -0.13 | -0.09 | -0.07 | -1.10 | 0.45 | -0.11 | -0.83 | -0.13 | -0.24 |
|  | (1.05) | (3.02) | (2.09) | (2.61) | (1.61) | (3.27) | (1.08) | (6.00) | (1.90) | (0.22) |
| Unemployment per capita | 3696.10 | 3579.56 | 2176.27 | -428.94 | 64903.00 | -776.94 | $1364.63$ | -263.53 | -1411.85 | -11388.00 |
|  | (5.14) | (4.06) | (2.49) | (0.78) | (4.49) | (0.99) | (2.36) | (0.33) | (3.50) | (1.76) |
| Poverty per capita (mov. avg) | -423.37 | $1986.23$ | -475.37 | 564.92 | -6773.10 | 1586.30 | 1065.55 | 214.04 | 391.89 | -1617.04 |
|  | (1.18) | (4.49) | (1.08) | (2.05) | (0.93) | (4.24) | (3.89) | (0.56) | (2.05) | (0.53) |
| Interaction (Mo*Population Density) | -0.02 | 0.00 | 0.08 | 0.12 | 2.89 | -0.08 | -0.32 | -0.14 | -0.36 | 1.33 |
|  | (0.54) | (0.10) | (2.15) | (5.35) | (4.95) | (0.36) | (1.91) | (0.59) | (3.07) | (0.71) |
| Interaction (Mo*Unemployment per capita) | $6096.42$ | $7486.71$ | $15447.00$ | 9434.72 | $152898.00$ | $2272.19$ | 3911.47 | 6396.72 | 22101.00 | 203268.00 |
|  | (1.57) | (1.57) | (3.27) | (3.18) | (1.96) | (0.43) | (1.00) | (1.18) | (8.12) | (4.66) |
| Interaction (Mo*Poverty per capita (mov. avg.)) | 1977.62 | 15.48 | -1898.51 | $7603.80$ | $126426.00$ | 5080.15 | 828.04 | 4326.32 | 2477.20 | 55240.00 |
|  | (1.21) | (0.01) | (0.95) | (6.08) | (3.84) | (2.04) | (0.45) | (1.71) | (1.94) | (2.70) |
| Interaction (Ms1*Population Density) | 0.00 | 0.00 | 0.00 | 0.00 | -0.03 | 0.03 | 0.02 | 0.01 | 0.03 | -0.11 |
|  | (2.24) | (1.46) | (1.08) | (4.02) | (3.23) | (5.26) | (5.24) | (2.23) | (11.23) | (2.62) |
| Interaction <br> (Ms1*Unemployment per capita) | -74.08 | -120.42 | 268.98 | -113.06 | -942.89 | -117.19 | 12.69 | -236.37 | -156.45 | 1853.43 |
|  | (1.32) | (1.75) | (3.93) | (2.63) | (0.83) | (0.70) | (0.10) | (1.39) | (1.82) | (1.35) |
| Interaction (Ms1*Poverty per capita (mov. avg.)) | -70.39 | 17.93 | -24.87 | 10.34 | 4182.01 | -349.18 | -64.17 | -235.30 | -253.57 | -1150.67 |
|  | (1.98) | (0.41) | (0.57) | (0.38) | (5.83) | (2.92) | (0.73) | (1.94) | (4.15) | (1.17) |
| Interaction (Ms2*Population Density) | 0.00 | 0.00 | 0.00 | 0.00 | -0.01 | -0.02 | 0.01 | 0.01 | 0.00 | 0.01 |
|  | (0.96) | (0.39) | (0.37) | (0.53) | (0.36) | (5.35) | (3.77) | (4.22) | (0.48) | (0.43) |

## Exhibit A-6(1) (continued) <br> SWS Model 2B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 - |  |  |  |  | 2 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Interaction (Ms2*Unemployment per capita) | -380.42 | 215.88 | 332.11 | 263.41 | -4419.10 | -247.66 | 26.56 | 56.74 | -7.86 | 448.18 |
|  | (4.40) | (2.03) | (3.15) | (3.98) | (2.54) | (7.59) | (1.11) | (1.71) | (0.47) | (1.67) |
| Interaction (Ms2*Poverty per capita (mov. avg.)) | -59.83 | 238.89 | 1.93 | -127.34 | 589.69 | 26.44 | -1.08 | 16.35 | 12.10 | 128.06 |
|  | (1.59) | (5.16) | (0.04) | (4.41) | (0.78) | (1.53) | (0.09) | (0.93) | (1.37) | (0.90) |
| Interaction (Ms3*Population Density) | 0.01 | -0.02 | -0.01 | -0.01 | -0.08 | 0.02 | -0.15 | -0.08 | -0.05 | 0.34 |
|  | (1.85) | (3.27) | (1.56) | (3.14) | (1.03) | (0.83) | (7.17) | (2.61) | (3.22) | (1.44) |
| Interaction (Ms3*Unemployment per capita) | -493.38 | $1520.46$ | -937.88 | -521.17 | 2610.11 | 2099.23 | 827.35 | 225.58 | -409.83 | -7860.33 |
|  | (1.39) | (3.49) | (2.17) | (1.92) | (0.37) | (4.47) | (2.41) | (0.47) | (1.71) | (2.04) |
| Interaction (Ms3*Poverty per capita (mov. avg.)) | 441.69 | 835.93 | 618.51 | 675.99 | 3820.93 | -915.06 | -652.55 | -194.62 | -71.16 | -1732.96 |
|  | (2.13) | (3.29) | (2.45) | (4.27) | (0.92) | (3.41) | (3.32) | (0.72) | (0.52) | (0.79) |

CA means Cash Assistance, M means Medicaid, NSS means Non-Health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending.

## Exhibit A-6(2)

SWS Model 2B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3 |  |  |  |  | 4 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Adjusted R-Squared | 0.90 | 0.92 | 0.93 | 0.91 | 0.97 | 0.59 | 0.96 | 0.92 | 0.97 | 0.96 |
| Constant | -71.16 | 147.48 | 169.92 | -8.00 | 4091.37 | 3.61 | 124.61 | 136.66 | -216.54 | 2217.86 |
|  | (2.02) | (2.16) | (2.75) | (0.11) | (8.95) | (0.05) | (1.55) | (2.55) | (3.62) | (3.00) |
| Per capita total income | 0.00 | 0.00 | 0.00 | 0.00 | 0.04 | 0.00 | 0.01 | 0.00 | 0.00 | 0.06 |
|  | (1.48) | (0.22) | (1.40) | (0.35) | (2.63) | (1.96) | (2.36) | (1.40) | (0.61) | (2.50) |
| Ratio of federal social welfare grants to cash assistance spending | 1.51 | -1.08 | 4.78 | 4.22 | -11.87 | 2.32 | -5.21 | -1.77 | -0.92 | -16.90 |
|  | (1.46) | (0.54) | (2.63) | (1.94) | (0.88) | (2.61) | (5.08) | -(2.59) | (1.21) | (1.79) |
| Ratio of federal social welfare grants to payment to medical vendors | -0.01 | 41.46 | -15.57 | 34.49 | 226.16 | -52.10 | 45.78 | 31.93 | 31.38 | 123.84 |
|  | (0.00) | (2.47) | -(1.03) | (1.90) | (2.02) | (2.87) | (2.18) | (2.28) | (2.00) | (0.64) |
| Ratio of federal social welfare grants to other welfare | 4.92 | 5.99 | -20.46 | 6.16 | 7.07 | 7.22 | 11.06 | -15.60 | 1.51 | 10.96 |
|  | (5.92) | (3.71) | -(14.02) | (3.53) | (0.65) | (6.19) | (8.21) | (17.32) | (1.50) | (0.88) |
| Ratio of federal non-social welfare grants to state-local spending on non-social welfare | 513.26 | 104.03 | 910.91 | -637.01 | -5771.48 | 635.68 | -193.71 | $160.43$ | 271.53 | $13594.00$ |
|  | (3.39) | (0.35) | (3.43) | (2.00) | (2.93) | (2.75) | (0.73) | -(0.90) | (1.36) | (5.52) |
| Ratio of federal non-social welfare grants to public hospital spending | -1.31 | -4.37 | 0.69 | 7.96 | 36.30 | -13.89 | -4.91 | 3.04 | -3.46 | 57.49 |
|  | (0.83) | (1.43) | (0.25) | (2.40) | (1.77) | (3.17) | (0.97) | (0.90) | (0.92) | (1.23) |
| Population Density | 0.47 | 0.03 | -0.65 | 0.03 | 0.31 | 1.03 | -0.86 | -0.36 | 2.79 | 17.92 |
|  | (2.54) | (0.09) | -(2.01) | (0.08) | (0.13) | (2.90) | (2.08) | -(1.31) | (9.07) | (4.71) |
| Unemployment per capita | 2830.31 | 884.94 | 1322.91 | -1495.57 | 31798.00 | 852.24 | $1672.20$ | $764.29$ | 381.28 | $27768.00$ |
|  | (6.43) | (1.03) | (1.71) | (1.62) | (5.56) | (0.89) | (1.52) | -(1.04) | (0.46) | (2.74) |
| Poverty per capita (mov. avg) | 273.93 | 442.63 | 155.85 | 185.28 | -8770.23 | 98.68 | 811.63 | 425.10 | 275.49 | -1221.92 |
|  | (1.61) | (1.34) | (0.52) | (0.52) | (3.96) | (0.51) | (3.61) | (2.83) | (1.64) | (0.59) |
| Interaction (Mo*Population Density) | 2.68 | 0.89 | -0.69 | 1.48 | -6.99 | -1.17 | -3.64 | 0.32 | 1.72 | -6.91 |
|  | (3.48) | (0.60) | -(0.51) | (0.92) | (0.70) | (0.88) | (2.36) | (0.31) | (1.49) | (0.49) |
| Interaction (Mo*Unemployment per capita) | $15461.00$ | $20845.00$ | $19249.00$ | 14199.00 | $164185.00$ | $4213.03$ | $2727.31$ | 404.85 | 3016.55 | 90800.00 |
|  | (4.70) | (3.27) | -(3.34) | (2.06) | (3.84) | (0.91) | (0.51) | (0.11) | (0.76) | (1.84) |

## Exhibit A-6(2) (continued) <br> SWS Model 2B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3 |  |  |  |  | 4 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
|  | (1.26) | (1.00) | -(0.20) | (0.92) | (4.36) | (3.01) | (1.81) | (0.17) | (0.73) | (3.31) |
| Interaction (Ms1*Population Density) | 0.00 | 0.02 | 0.00 | -0.03 | -0.17 | 0.07 | 0.15 | -0.01 | -0.12 | 1.39 |
|  | (0.34) | (1.83) | (0.20) | (2.40) | (1.85) | (1.31) | (2.54) | -(0.28) | (2.66) | (2.52) |
| Interaction <br> (Ms1*Unemployment per capita) | -19.62 | 50.34 | -93.86 | -54.43 | 318.98 | 125.98 | -215.79 | -14.63 | -14.48 | -1228.20 |
|  | (0.90) | (1.19) | -(2.45) | (1.19) | (1.12) | (1.27) | (1.88) | -(0.19) | (0.17) | (1.16) |
| Interaction (Ms1*Poverty per capita (mov. avg.)) | 11.96 | 23.77 | 7.01 | -48.81 | -295.86 | 59.31 | 67.45 | 5.22 | -67.01 | 111.46 |
|  | (1.10) | (1.13) | (0.37) | (2.14) | (2.10) | (1.81) | (1.78) | (0.21) | (2.37) | (0.32) |
| Interaction (Ms2*Population Density) | 0.01 | -0.01 | -0.02 | 0.01 | 0.07 | -0.01 | 0.05 | 0.02 | -0.01 | -0.13 |
|  | (2.59) | (1.25) | -(2.55) | (0.71) | (1.55) | (1.59) | (6.24) | (3.06) | (0.91) | (1.83) |
| Interaction (Ms2*Unemployment per capita) | -149.59 | 305.77 | 139.51 | -128.48 | -380.81 | -9.28 | 62.39 | 15.64 | 37.96 | 505.99 |
|  | (3.81) | (4.01) | (2.03) | (1.56) | (0.75) | (0.38) | (2.20) | (0.83) | (1.80) | (1.94) |
| Interaction (Ms2*Poverty per capita (mov. avg.)) | -13.22 | -29.63 | -52.42 | -38.31 | 97.24 | -14.14 | 8.03 | 3.75 | 4.03 | 93.83 |
|  | (1.53) | (1.77) | -(3.46) | (2.11) | (0.87) | (3.23) | (1.59) | (1.11) | (1.07) | (2.02) |
| Interaction (Ms3*Population Density) | -0.01 | 0.02 | 0.13 | -0.23 | -0.73 | 0.32 | -0.44 | -0.02 | -0.12 | 0.43 |
|  | (0.19) | (0.18) | (1.37) | (1.99) | (1.03) | (3.53) | (4.19) | -(0.28) | (1.54) | (0.45) |
| Interaction (Ms3*Unemployment per capita) | -108.19 | 479.07 | 454.76 | -49.79 | -3807.80 | -126.75 | 1187.03 | 274.43 | -660.91 | 8339.54 |
|  | (0.75) | (1.71) | (1.80) | (0.16) | (2.03) | (0.27) | (2.21) | (0.76) | (1.65) | (1.68) |
| Interaction (Ms3*Poverty per capita (mov. avg.)) | 30.37 | -662.09 | 12.55 | -118.25 | -1061.45 | 217.20 | -790.69 | $190.07$ | -33.21 | -3463.81 |
|  | (0.37) | (4.13) | (0.09) | (0.68) | (0.99) | (1.81) | (5.71) | -(2.05) | (0.32) | (2.72) |
| CA means Cash Assistance, M means Medicaid, NSS means Non-Health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending. |  |  |  |  |  |  |  |  |  |  |

## Model 3A Specification

The Model 3 series regressions all estimate the $\theta_{\mathrm{O}}$ and $\theta_{\mathrm{S}}$ parameters that determine the price effects of grants. Model 3A includes the estimated $\theta_{\mathrm{O}}$ and $\theta_{\mathrm{S}}$ parameters, but no flypaper effect parameters and no need variables, i.e., $\left(\Pi_{\mathrm{OS}}=\Pi_{\mathrm{OO}}=\Pi_{\mathrm{SS}}=\Pi_{\mathrm{SO}}=0\right)$, and $\left(\lambda_{\mathrm{Si}}=\lambda_{\mathrm{oi}}=\lambda_{\mathrm{yi}}=0\right)$. The model structure is:
$L_{S}+G_{S}=a_{1}+b_{1} R_{L}+c_{1} G_{O}+d_{1} G_{S}+e_{1} M_{S}+f_{1} M_{O}$
$\mathrm{L}_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2} \mathrm{R}_{\mathrm{L}}+\mathrm{c}_{2} \mathrm{G}_{\mathrm{O}}+\mathrm{d}_{2} \mathrm{G}_{\mathrm{S}}+\mathrm{e}_{2} \mathrm{M}_{\mathrm{S}}+\mathrm{f}_{2} \mathrm{M}_{\mathrm{O}}$
$Y=a_{3}+b_{3} R_{L}+c_{3} G_{o}+d_{3} G_{S}+e_{3} M_{S}+f_{3} M_{o}$
The regression results for Model 3A are reported in Exhibit A-7.

## Exhibit A-7

SWS Model 3A Coefficient Estimates With Year Dummies

| Variable | Overall |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | CA | M | NSS | PH | NSWS |
| Adjusted R-Squared | 0.87 | 0.95 | 0.93 | 0.89 | 0.96 |
| Constant | 111.97 | -21.84 | 57.54 | 159.05 | 4045.78 |
|  | (5.57) | (1.20) | (3.15) | (8.00) | (14.60) |
| Per capita total income | -0.01 | 0.00 | 0.00 | 0.00 | 0.07 |
|  | (9.37) | (6.04) | (4.71) | (1.13) | (9.58) |
| Federal grants for non-social welfare | 0.04 | -0.01 | 0.05 | 0.08 | 1.99 |
|  | (3.95) | (1.45) | (4.64) | (6.85) | (12.71) |
| Federal grants for social welfare | 0.06 | 0.36 | 0.22 | 0.08 | -0.06 |
|  | (5.02) | (33.84) | (21.20) | (7.23) | (0.36) |
| Ratio of federal social welfare grants to cash assistance spending | -0.84 | 0.06 | -0.03 | 0.26 | -1.68 |
|  | (9.00) | (0.68) | (0.31) | (2.85) | (1.30) |
| Ratio of federal social welfare grants to payment to medical vendors | -3.27 | -42.45 | 0.15 | 2.65 | -5.93 |
|  | (1.90) | (27.34) | (0.10) | (1.56) | (0.25) |
| Ratio of federal social welfare grants to other welfare | 4.21 | 1.13 | -31.45 | 3.32 | -35.65 |
|  | (4.09) | (1.22) | (33.62) | (3.26) | (2.51) |
| Ratio of federal non-social welfare grants to state-local spending on non-social welfare | -86.33 | 27.86 | -132.55 | -348.85 | -11281.00 |
|  | (1.56) | (0.56) | (2.63) | (6.36) | (14.75) |
| Ratio of federal non-social welfare grants to public hospital spending | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 |
|  | (0.17) | (1.64) | (6.04) | (2.04) | (0.89) |

CA means Cash Assistance, M means Medicaid, NSS means Non-Health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending.

## Exhibit A-7(1)

SWS Model 3A Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 |  |  |  |  | 2 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Adjusted RSquared | 0.91 | 0.95 | 0.94 | 0.91 | 0.96 | 0.73 | 0.96 | 0.94 | 0.96 | 0.98 |
| Constant | 301.81 | -53.73 | 188.46 | 10.80 | 3951.82 | -90.00 | 197.79 | 89.00 | 253.51 | 5566.09 |
|  | (9.18) | (1.56) | (5.78) | (0.39) | (5.47) | (1.02) | (4.85) | (1.59) | (6.82) | (12.89) |
| Per capita total income | -0.01 | 0.00 | 0.00 | 0.00 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
|  | (7.85) | (2.88) | (0.68) | (4.77) | (4.11) | (1.11) | (0.95) | (0.72) | (3.95) | (0.28) |
| Federal grants for non-social welfare | 0.02 | -0.02 | 0.14 | 0.10 | 2.41 | 0.08 | -0.03 | 0.04 | 0.18 | 3.70 |
|  | (1.23) | (0.74) | (7.31) | (6.04) | (5.51) | (1.63) | (1.39) | (1.29) | (8.91) | (15.49) |
| Federal grants for social welfare | 0.08 | 0.44 | 0.27 | 0.06 | -0.90 | 0.01 | 0.24 | 0.30 | 0.07 | 0.22 |
|  | (3.52) | (19.40) | (12.37) | (3.22) | (1.90) | (0.36) | (12.78) | (11.70) | (4.27) | (1.11) |
| Ratio of federal social welfare grants to cash assistance spending | -3.88 | 0.03 | 1.51 | -0.80 | -5.25 | -1.61 | -0.15 | -0.17 | 0.17 | -6.64 |
|  | (3.91) | (0.03) | (1.53) | (0.96) | (0.24) | (5.07) | (0.99) | (0.84) | (1.28) | (4.28) |
| Ratio of federal social welfare grants to payment to medical vendors | 4.94 | -50.82 | -0.22 | -4.98 | -156.18 | -4.95 | -75.00 | 1.81 | -1.14 | 84.23 |
|  | (1.02) | (10.05) | (0.05) | (1.23) | (1.47) | (0.62) | (20.44) | (0.36) | (0.34) | (2.17) |
| Ratio of federal social welfare grants to other welfare | 11.62 | 1.37 | -48.38 | 1.45 | -23.36 | 10.46 | 5.14 | -48.88 | -3.82 | -54.24 |
|  | (3.90) | (0.44) | (16.35) | (0.58) | (0.36) | (2.37) | (2.52) | (17.45) | (2.05) | (2.51) |
| Ratio of federal non-social welfare grants to statelocal spending on non-social welfare | 109.11 | $141.20$ | $876.91$ | $266.41$ | -14527.00 | $164.36$ | 76.57 | 50.43 | $404.48$ | -18236.00 |
|  | (0.86) | (1.06) | (6.97) | (2.50) | (5.21) | (1.00) | (1.01) | (0.48) | (5.86) | (22.76) |
| Ratio of federal non-social welfare grants to public hospital spending | 1.20 | 4.99 | -0.70 | -9.79 | -69.92 | -6.00 | -6.31 | -0.28 | -23.21 | 28.46 |
|  | (1.15) | (4.60) | (0.68) | (11.23) | (3.06) | (2.16) | (4.91) | (0.16) | (19.83) | (2.09) |

CA means Cash Assistance, M means Medicaid, NSS means Non-Health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending.

Exhibit A-7(2)
SWS Model 3A Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3 |  |  |  |  | 4 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Adjusted R-Squared | 0.84 | 0.95 | 0.95 | 0.90 | 0.98 | 0.54 | 0.97 | 0.96 | 0.96 | 0.98 |
| Constant | $39.53$ | -31.41 | 31.21 | $208.54$ | 3152.41 | 171.73 | -61.50 | 88.79 | $129.62$ | 3152.27 |
|  | (1.27) | (0.83) | (0.84) | (3.73) | (12.27) | (4.58) | (1.80) | (4.70) | (3.45) | (11.74) |
| Per capita total income | 0.00 | 0.00 | 0.00 | 0.00 | 0.03 | 0.00 | 0.01 | 0.00 | 0.01 | 0.00 |
|  | (2.62) | (1.35) | (0.42) | (1.84) | (4.07) | (1.83) | (4.57) | (2.29) | (5.80) | (0.04) |
| Federal grants for non-social welfare | -0.02 | 0.06 | 0.06 | 0.05 | 3.50 | 0.02 | 0.08 | 0.00 | 0.05 | 5.42 |
|  | (0.58) | (1.79) | (2.02) | (1.08) | (16.48) | (0.59) | (2.27) | (0.06) | (1.41) | (19.73) |
| Federal grants for social welfare | 0.11 | 0.36 | 0.31 | 0.10 | -0.14 | -0.08 | 0.37 | 0.19 | -0.02 | 0.14 |
|  | (6.09) | (16.93) | (14.57) | (3.04) | (0.97) | (4.18) | (20.38) | (19.03) | (0.98) | (0.99) |
| Ratio of federal social welfare grants to cash assistance spending | -0.54 | 0.09 | 0.51 | 0.18 | 2.04 | -0.59 | 0.02 | -0.15 | 0.24 | -1.46 |
|  | (4.94) | (0.67) | (3.95) | (0.92) | (2.27) | (6.73) | (0.19) | -(3.51) | (2.77) | (2.34) |
| Ratio of federal social welfare grants to payment to medical vendors | -3.04 | -26.77 | -0.47 | 8.67 | -30.82 | -2.24 | -86.92 | 2.15 | 6.02 | -51.69 |
|  | (2.47) | (17.94) | (0.32) | (3.93) | (3.04) | (0.55) | (23.48) | (1.05) | (1.48) | (1.78) |
| Ratio of federal social welfare grants to other welfare | 3.11 | -0.42 | -26.05 | 4.25 | 10.72 | 8.74 | 1.57 | -22.10 | 5.33 | -1.56 |
|  | (3.14) | (0.35) | (21.97) | (2.39) | (1.31) | (6.56) | (1.29) | (32.94) | (3.99) | (0.16) |
| Ratio of federal nonsocial welfare grants to state-local spending on nonsocial welfare | 42.49 | $187.16$ | 265.74 | -9.36 | -11440.00 | $258.38$ | -60.68 | -42.96 | 154.33 | -15370.00 |
|  | (0.52) | (1.88) | (2.71) | (0.06) | (16.92) | (2.40) | (0.62) | -(0.79) | (1.43) | (19.96) |
| Ratio of federal nonsocial welfare grants to public hospital spending | 0.00 | 0.00 | 0.00 | 0.00 | -0.01 | -0.25 | -2.07 | 0.64 | -18.85 | -33.84 |
|  | (0.66) | (1.62) | (5.77) | (1.97) | (2.34) | (0.15) | (1.39) | (0.78) | (11.49) | (2.89) |

CA means Cash Assistance, M means Medicaid, NSS means Non-Health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending.

## Model 3B Specification

Model 3B adds need variables to the structure of Model 3A. The model structure is the full reduced form:
$L_{s}+G_{S}=a_{1}+b_{1} R_{L}+c_{1} G_{o}+d_{1} G_{S}+e_{1} M_{S}+f_{1} M_{o}+\sum g_{1 i} x_{i}+\sum h_{1 i} x_{i} M_{s}+\sum \varphi_{1 i} x_{i} M_{o}$
$\mathrm{L}_{\mathrm{O}}+\mathrm{G}_{\mathrm{O}}=\mathrm{a}_{2}+\mathrm{b}_{2} \mathrm{R}_{\mathrm{L}}+\mathrm{c}_{2} \mathrm{G}_{\mathrm{O}}+\mathrm{d}_{2} \mathrm{G}_{\mathrm{s}}+\mathrm{e}_{2} \mathrm{M}_{\mathrm{s}}+\mathrm{f}_{2} \mathrm{M}_{\mathrm{O}}+\sum \mathrm{g} 2 \mathrm{i} \mathrm{X}_{\mathrm{i}}+\sum \mathrm{h}_{2 \mathrm{i}} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{S}}+\sum \varphi_{2 \mathrm{i}} \mathrm{X}_{\mathrm{i}} \mathrm{M}_{\mathrm{o}}$
$Y=a_{3}+b_{3} R_{L}+c_{3} G_{O}+d_{3} G_{S}+e_{3} M_{S}+f_{3} M_{o}+\sum g_{2 i} X_{i}+\sum h_{2 i} X_{i} M_{S}+\sum \varphi_{2 i} X_{i} M_{o}$

The results are reported in Exhibit A-8.

## Exhibit A-8

SWS Model 3B Coefficient Estimates With Year Dummies

| Variable | Overall |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | CA | M | NSS | PH | NSWS |
| Adjusted R-Squared | 0.89 | 0.96 | 0.94 | 0.92 | 0.97 |
| Constant | 22.96 | -19.99 | 65.13 | 82.44 | 3818.76 |
|  | (0.89) | (0.87) | (2.66) | (3.31) | (10.48) |
| Per capita personal income | 0.00 | 0.00 | 0.00 | 0.00 | 0.09 |
|  | (3.56) | (4.66) | (3.21) | (1.84) | (9.81) |
| Federal grants for non-social welfare | 0.01 | -0.04 | 0.05 | 0.12 | 2.34 |
|  | (0.78) | (3.21) | (3.91) | (8.70) | (11.87) |
| Federal grants for social welfare | 0.10 | 0.33 | 0.24 | 0.06 | 0.18 |
|  | (8.29) | (29.11) | (19.95) | (4.89) | (1.02) |
| Ratio of federal social welfare grants to cash assistance spending | 2.14 | 0.52 | 1.03 | 0.74 | 5.56 |
|  | (5.76) | (1.58) | (2.92) | (2.08) | (1.06) |
| Ratio of federal social welfare grants to payment to medical vendors | -16.19 | -6.51 | -23.33 | 8.45 | -65.05 |
|  | (2.30) | (1.04) | (3.49) | (1.24) | (0.65) |
| Ratio of federal social welfare grants to other welfare | 3.92 | 2.85 | -30.38 | 3.69 | -21.32 |
|  | (3.95) | (3.23) | (32.32) | (3.86) | (1.52) |
| Ratio of federal non-social welfare grants to state-local spending on nonsocial welfare | 72.89 | -21.73 | 69.77 | -327.33 | -14948.00 |
|  | (0.81) | (0.27) | (0.81) | (3.75) | (11.70) |
| Ratio of federal non-social welfare grants to public hospital spending | 0.07 | 0.26 | -1.36 | 1.31 | -13.45 |
|  | (0.12) | (0.54) | (2.64) | (2.49) | (1.75) |
| Population Density | -0.03 | -0.03 | 0.00 | 0.02 | 1.23 |
|  | (1.17) | (1.33) | (0.11) | (0.74) | (4.07) |
| Unemployment per capita | 1774.34 | 787.79 | 408.07 | -530.14 | 33010.00 |
|  | (5.73) | (2.85) | (1.39) | (1.78) | (7.55) |
| Poverty per capita (mov. avg) | -111.98 | 78.49 | -243.34 | 292.66 | -9686.37 |
|  | (1.16) | (0.91) | (2.66) | (3.15) | (7.11) |
| Interaction (Mo*Population Density) | 0.02 | 0.01 | 0.01 | 0.00 | -1.11 |
|  | (1.67) | (0.99) | (0.61) | (0.37) | (5.79) |
| Interaction (Mo*Unemployment per capita) | -3155.00 | -2795.09 | -8151.64 | 8829.82 | -181072.00 |
|  | (1.72) | (1.71) | (4.68) | (4.98) | (6.98) |
| Interaction (Mo*Poverty per capita (mov. avg.)) | -215.26 | 1512.26 | 216.09 | -1827.09 | 65465.00 |
|  | (0.41) | (3.23) | (0.43) | (3.61) | (8.84) |
| Interaction (Ms1*Population Density) | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 |
|  | (0.26) | (2.40) | (3.65) | (6.03) | (2.00) |
| Interaction (Ms1*Unemployment per capita) | -99.02 | 43.44 | 131.44 | -214.84 | -504.20 |
|  | (3.87) | (1.90) | (5.42) | (8.71) | (1.40) |
| Interaction (Ms1*Poverty per capita (mov. avg.)) | 12.40 | -7.59 | -7.05 | 18.48 | 163.60 |
|  | (3.47) | (2.38) | (2.08) | (5.37) | (3.25) |
| Interaction (Ms2*Population Density) | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
|  | (2.76) | (2.78) | (4.80) | (2.52) | (0.25) |

## Exhibit A-8 (continued) <br> SWS Model 3B Coefficient Estimates With Year Dummies

| Variable | Overall |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | CA | M | NSS | PH | NSWS |
| Interaction (Ms2*Unemployment per capita) | -183.95 | 31.56 | 13.57 | 0.54 | -696.04 |
|  | (9.95) | (1.92) | (0.77) | (0.03) | (2.67) |
| Interaction (Ms2*Poverty per capita (mov. avg.)) | 8.74 | -7.62 | -9.44 | -2.66 | 73.28 |
|  | (3.11) | (3.03) | (3.54) | (0.98) | (1.84) |
| Interaction (Ms3*Population Density) | 0.01 | -0.02 | -0.01 | 0.00 | 0.13 |
|  | (2.71) | (10.20) | (2.87) | (0.82) | (3.44) |
| Interaction (Ms3*Unemployment per capita) | 344.93 | -53.17 | 79.48 | 144.95 | 1125.23 |
|  | (2.21) | (0.38) | (0.54) | (0.96) | (0.51) |
| Interaction (Ms3*Poverty per capita (mov. avg.)) | 10.91 | -255.47 | 196.96 | -98.23 | 92.08 |
|  | (0.20) | (5.19) | (3.76) | (1.85) | (0.12) |

CA means Cash Assistance, M means Payments to Medicaid, NSS means Non-Health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending.

Exhibit A-8(1)
SWS Model 3B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 |  |  |  |  | 2 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Adjusted R-Squared | 0.94 | 0.97 | 0.96 | 0.95 | 0.97 | 0.87 | 0.98 | 0.96 | 0.98 | 0.99 |
| Constant | 137.53 | 72.54 | 102.79 | -99.75 | 476.85 | -225.43 | 65.29 | 56.78 | 104.03 | 4010.85 |
|  | (3.13) | (1.71) | (2.22) | (3.00) | (0.51) | (2.75) | (1.60) | (0.92) | (2.80) | (8.21) |
| Per capita personal income | -0.01 | 0.00 | 0.00 | 0.01 | 0.16 | 0.01 | 0.00 | 0.00 | 0.00 | 0.03 |
|  | (6.03) | (4.84) | (2.20) | (7.38) | (8.24) | (3.03) | (1.98) | (2.93) | (0.56) | (2.35) |
| Federal grants for non-social welfare | 0.03 | -0.10 | 0.09 | 0.11 | 2.51 | -0.05 | -0.09 | -0.01 | 0.18 | 3.86 |
|  | (1.29) | (5.29) | (4.35) | (7.18) | (5.75) | (1.07) | (3.56) | (0.15) | (8.26) | (13.30) |
| Federal grants for social welfare | 0.21 | 0.39 | 0.34 | 0.10 | 0.97 | 0.05 | 0.29 | 0.36 | 0.00 | 0.72 |
|  | (8.23) | (15.81) | (12.54) | (4.98) | (1.79) | (1.32) | (17.42) | (14.22) | (0.04) | (3.53) |
| Ratio of federal social welfare grants to cash assistance spending | 19.22 | -10.87 | 11.18 | 12.07 | 85.64 | 1.34 | 1.46 | 0.04 | 0.76 | 9.92 |
|  | (5.56) | (3.27) | (3.07) | (4.62) | (1.17) | (0.72) | (1.58) | (0.03) | (0.90) | (0.89) |
| Ratio of federal social welfare grants to payment to medical vendors | -35.64 | -100.29 | -41.75 | -55.02 | -468.60 | 19.03 | -20.95 | 4.22 | 13.16 | 206.47 |
|  | (2.04) | (5.96) | (2.26) | (4.16) | (1.26) | (0.74) | (1.65) | (0.22) | (1.14) | (1.35) |
| Ratio of federal social welfare grants to other welfare | 2.78 | 5.14 | -49.58 | -3.99 | -138.94 | 13.29 | 4.08 | -49.94 | -0.55 | -77.51 |
|  | (1.04) | (2.01) | (17.69) | (1.99) | (2.46) | (4.20) | (2.60) | (21.10) | (0.39) | (4.12) |

## Exhibit A-8(1) (continued) SWS Model 3B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 , |  |  |  |  | 2 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Ratio of federal non-social welfare grants to statelocal spending on non-social welfare | -80.54 | 473.15 | -116.54 | 195.25 | -4880.26 | -382.01 | -77.36 | -603.72 | -525.57 | -17688.00 |
|  | (0.45) | (2.75) | (0.62) | (1.44) | (1.28) | (1.49) | (0.61) | (3.14) | (4.53) | (11.58) |
| Ratio of federal non-social welfare grants to public hospital spending | 3.91 | 2.89 | -9.23 | -7.29 | -423.17 | 24.32 | -13.95 | 22.10 | -12.24 | 28.19 |
|  | (1.36) | (1.04) | (3.05) | (3.36) | (6.93) | (2.03) | (2.35) | (2.47) | (2.26) | (0.40) |
| Population Density | -0.02 | -0.06 | -0.06 | -0.08 | -1.42 | 0.52 | 0.25 | -0.45 | -0.22 | -1.35 |
|  | (0.50) | (2.10) | (1.95) | (3.28) | (2.19) | (3.59) | (3.43) | (4.10) | (3.37) | (1.56) |
| Unemployment per capita | 2888.75 | 2182.55 | 848.60 | -859.22 | 59706.00 | -858.77 | -1177.14 | 250.51 | -899.10 | 542.35 |
|  | (4.47) | (3.51) | (1.25) | (1.76) | (4.35) | (1.07) | (2.97) | (0.42) | (2.49) | (0.11) |
| Poverty per capita (mov. avg) | -183.02 | -1649.62 | -53.60 | 744.23 | -3994.31 | 1409.49 | 353.36 | -489.44 | 707.80 | 3684.03 |
|  | (0.57) | (5.33) | (0.16) | (3.06) | (0.58) | (3.59) | (1.82) | (1.67) | (3.99) | (1.58) |
| Interaction (Mo*Population Density) | 0.00 | 0.12 | 0.08 | 0.07 | 1.65 | -0.08 | -0.04 | 0.33 | -0.14 | 6.83 |
|  | (0.05) | (4.38) | (2.52) | (3.34) | (2.74) | (0.35) | (0.31) | (1.88) | (1.34) | (4.84) |
| Interaction (Mo*Unemployment per capita) | -3192.52 | -1592.60 | -10962.00 | 10421.00 | -147711.00 | -2010.94 | 28.63 | -577.21 | 18136.00 | 104983.00 |
|  | (0.92) | (0.48) | (3.00) | (3.98) | (2.01) | (0.37) | (0.01) | (0.14) | (7.39) | (3.25) |
| Interaction (Mo*Poverty per capita (mov. avg.)) | 1214.36 | -2930.94 | -2610.17 | -6960.52 | -106085.00 | 6512.00 | 3814.71 | 5508.00 | -2052.21 | -38655.00 |
|  | (0.82) | (2.07) | (1.68) | (6.25) | (3.39) | (2.34) | (2.76) | (2.64) | (1.63) | (2.33) |
| Interaction (Ms1*Population Density) | 0.00 | 0.00 | 0.00 | 0.00 | -0.02 | 0.02 | 0.00 | -0.01 | 0.03 | -0.12 |
|  | (1.23) | (2.77) | (2.15) | (2.73) | (1.57) | (4.04) | (0.69) | (3.24) | (12.13) | (3.45) |
| Interaction (Ms1*Unemployment per capita) | -69.57 | -50.13 | 255.51 | -151.01 | -1884.51 | -92.55 | 80.04 | -190.13 | -223.10 | 529.74 |
|  | (1.37) | (1.03) | (4.79) | (3.95) | (1.75) | (0.55) | (0.96) | (1.51) | (2.92) | (0.53) |
| Interaction (Ms1*Poverty per capita (mov. avg.)) | -38.61 | 85.76 | 23.09 | 18.98 | 4187.00 | -340.80 | 66.75 | -44.19 | -199.66 | 379.03 |
|  | (1.21) | (2.79) | (0.69) | (0.79) | (6.17) | (2.82) | (1.11) | (0.49) | (3.65) | (0.53) |
| Interaction (Ms2*Population Density) | 0.00 | 0.00 | 0.00 | 0.00 | -0.02 | -0.02 | 0.00 | 0.00 | 0.00 | 0.03 |
|  | (1.01) | (2.75) | (3.80) | (1.19) | (1.27) | (5.55) | (0.19) | (1.72) | (1.87) | (1.83) |
| Interaction (Ms2*Unemployment per capita) | -485.42 | 25.42 | 162.37 | 213.11 | -4958.72 | -245.11 | 17.30 | 35.15 | -26.30 | 12.96 |
|  | (6.23) | (0.34) | (1.98) | (3.62) | (2.99) | (7.44) | (1.06) | (1.42) | (1.76) | (0.07) |

## Exhibit A-8(1) (continued) SWS Model 3B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 |  |  |  |  | 2 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Interaction (Ms2*Poverty per capita (mov. avg.)) | $130.87$ | 114.26 |  | 114.32-164.10 | 158.96 | 26.38 | -16.49 | -8.52 | 1.46 | -147.95 |
|  | (3.79) | (3.44) | (3.14) | (6.28) | (0.22) | (1.50) | (1.90) | (0.65) | (0.18) | (1.42) |
| Interaction (Ms3*Population Density) | 0.00 | -0.03 | -0.01 | 0.00 | 0.06 | 0.03 | -0.15 | -0.08 | -0.06 | 0.09 |
|  | (0.59) | (9.57) | (2.96) | (1.71) | (0.71) | (0.93) | (10.25) | (3.58) | (4.52) | (0.53) |
| Interaction (Ms3*Unemployment per capita) | 19.68-901.24 |  | -4.37 | -74.26 | 10084.00 | 2125.49 | 1078.74 | 566.52 | -353.50-5978.16 |  |
|  | (0.06) | (2.90) | (0.01) | (0.30) | (1.47) | (4.52) | (4.63) | (1.61) | (1.66) | (2.14) |
| Interaction (Ms3*Poverty per capita (mov. avg.)) | 394.94 | 951.42 | 475.98 | 524.23 | 469.40 | -935.63 | -637.76 | -117.92 | 34.79 | 673.00 |
|  | (2.13) | (5.32) | (2.43) | (3.73) | (0.12) | (3.48) | (4.78) | (0.59) | (0.29) | (0.42) |

CA means Cash Assistance, M means Payments to Medicaid, NSS means Non-Health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending.

## Exhibit A-8(2)

SWS Model 3B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3 |  |  |  |  | 4 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Adjusted R-Squared | 0.93 | 0.97 | 0.96 | 0.92 | 0.99 | 0.59 | 0.98 | 0.96 | 0.97 | 0.99 |
| Constant | -140.04 | -46.57 | 21.12 | -90.43 | 3969.83 | 14.45 | 66.57 | 93.73 | -200.84 | 2718.54 |
|  | (4.58) | (1.07) | (0.44) | (1.26) | (11.89) | (0.21) | (1.28) | (2.53) | (3.39) | (7.42) |
| Per capita personal income | 0.00 | 0.00 | 0.00 | 0.00 | 0.03 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 |
|  | (1.38) | (0.24) | (1.37) | (0.12) | (3.07) | (1.97) | (2.85) | (1.83) | (0.36) | (0.17) |
| Federal grants for non-social welfare | 0.03 | -0.02 | 0.06 | 0.14 | 4.05 | 0.01 | 0.10 | 0.01 | 0.05 | 5.54 |
|  | (1.47) | (0.47) | (1.71) | (2.46) | (15.81) | (0.28) | (3.44) | (0.48) | (1.35) | (26.86) |
| Federal grants for social welfare | 0.13 | 0.37 | 0.28 | 0.15 | -0.03 | -0.05 | 0.33 | 0.21 | -0.05 | 0.19 |
|  | (10.02) | (20.27) | (13.90) | (4.89) | (0.23) | (1.91) | (17.77) | (16.11) | (2.59) | (1.50) |
| Ratio of federal social welfare grants to cash assistance spending | 2.20 | 0.81 | 6.27 | 5.09 | -8.75 | 1.77 | -1.05 | 0.82 | -1.50 | -4.00 |
|  | (2.50) | (0.64) | (4.55) | (2.45) | (0.91) | (1.89) | (1.50) | (1.64) | (1.88) | (0.81) |
| Ratio of federal social welfare grants to payment to medical vendors | -0.74 | 48.30 | -16.22 | 26.16 | -90.26 | -40.95 | -31.59 | -18.15 | 44.29 | 80.05 |
|  | (0.10) | (4.51) | (1.38) | (1.47) | (1.10) | (2.16) | (2.22) | (1.79) | (2.73) | (0.80) |
| Ratio of federal social welfare grants to other welfare | 3.04 | 0.45 | -24.55 | 4.10 | 11.86 | 8.62 | 1.68 | -21.77 | 3.18 | 15.47 |
|  | (4.16) | (0.44) | (21.52) | (2.38) | (1.49) | (6.30) | (1.65) | (29.80) | (2.73) | (2.14) |
| Ratio of federal non-social welfare grants to state-local spending on nonsocial welfare | 191.12 | -459.57 | 251.14 | -1310.35 | -18502.00 | 607.85 | -357.08 | $155.15$ | 174.23 | $24736.00$ |
|  | (1.28) | (2.16) | (1.07) | (3.72) | (11.32) | (2.50) | (1.96) | (1.19) | (0.84) | (19.28) |
| Ratio of federal non-social welfare grants to public hospital spending | -1.36 | -3.34 | 0.70 | 6.92 | -5.30 | -14.04 | -4.24 | 3.58 | -3.70 | 46.64 |
|  | (1.00) | (1.73) | (0.33) | (2.16) | (0.36) | (3.22) | (1.30) | (1.54) | (0.99) | (2.03) |
| Population Density | 0.59 | 0.43 | -0.37 | 0.15 | -0.91 | 0.93 | -0.43 | 0.01 | 2.62 | 8.78 |
|  | (3.79) | (1.93) | (1.52) | (0.40) | (0.54) | (2.54) | (1.57) | (0.06) | (8.40) | (4.57) |
| Unemployment per capita | 2031.46 | -431.04 | $304.61$ | -3233.63 | -2658.18 | 697.83 | 120.74 | 171.55 | 334.24 | -4380.95 |
|  | (4.76) | (0.71) | (0.46) | (3.22) | (0.57) | (0.72) | (0.17) | (0.33) | (0.40) | (0.86) |
| Poverty per capita (mov. avg) | 244.76 | 297.34 | 86.21 | 203.20 | -6589.54 | 232.38 | -152.22 | $187.55$ | 423.68 | -2892.32 |
|  | (1.69) | (1.45) | (0.38) | (0.60) | (4.16) | (1.12) | (0.98) | (1.70) | (2.40) | (2.65) |
| Interaction (Mo*Population Density) | 2.57 | 0.10 | -0.99 | 1.73 | 9.23 | -1.25 | -2.11 | 1.01 | 1.80 | 23.48 |
|  | (3.89) | (0.11) | (0.96) | (1.11) | (1.28) | (0.93) | (2.09) | (1.40) | (1.56) | (3.30) |
| Interaction (Mo*Unemployment per capita) | -6146.77 | -1902.15 | 105.99 | 31453.00 | 110325.00 | $4064.65$ | $5825.55$ | $956.30$ | 2810.62 | 24911.00 |
|  | (1.87) | (0.41) | (0.02) | (4.06) | (3.07) | (0.88) | (1.68) | (0.39) | (0.71) | (1.02) |
| Interaction (Mo*Poverty per capita (mov. avg.)) | -1246.46 | 3988.33 | 173.01 | 1529.68 | 24976.00 | $3390.56$ | 2770.69 | 452.32 | -777.01 | 38523.00 |
|  | (1.24) | (2.79) | (0.11) | (0.64) | (2.27) | (3.08) | (3.37) | (0.77) | (0.83) | (6.64) |
| Interaction (Ms1*Population Density) | 0.00 | 0.02 | 0.00 | -0.03 | 0.02 | 0.07 | 0.07 | -0.05 | -0.12 | -0.16 |
|  | (0.28) | (2.04) | (0.04) | (2.22) | (0.36) | (1.37) | (1.76) | (1.75) | (2.70) | (0.57) |

## Exhibit A-8(2) (continued) <br> SWS Model 3B Coefficient Estimates With Year Dummies

| Variable | Quartile |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 O |  |  |  |  | 2 |  |  |  |  |
|  | CA | M | NSS | PH | NSWS | CA | M | NSS | PH | NSWS |
| Interaction (Ms1*Unemployment per capita) | -19.82 | 67.62 | -92.41 | -69.59 | -312.06 | 112.35 | -98.92 | 54.09 | -26.20 | -471.66 |
|  | (1.05) | (2.52) | (3.14) | (1.56) | (1.51) | (1.13) | (1.33) | (1.02) | (0.31) | (0.90) |
| Interaction (Ms1*Poverty per capita (mov. avg.)) | 12.41 | 14.49 | 6.87 | -39.45 | 77.80 | 64.96 | 21.85 | -22.30 | -61.63 | -112.85 |
|  | (1.31) | (1.08) | (0.47) | (1.78) | (0.76) | (1.98) | (0.89) | (1.27) | (2.20) | (0.65) |
| Interaction (Ms2*Population Density) | 0.01 | -0.01 | -0.02 | 0.01 | 0.08 | -0.01 | 0.02 | -0.01 | 0.00 | 0.12 |
|  | (3.07) | (2.07) | (3.36) | (0.80) | (2.56) | (0.73) | (3.66) | (1.27) | (0.38) | (2.93) |
| Interaction (Ms2*Unemployment per capita) | -201.05 | 145.08 | 26.70 | -176.90 | 84.35 | -6.19 | 22.15 | -4.57 | 38.12 | -98.04 |
|  | (5.95) | (3.02) | (0.51) | (2.22) | (0.23) | (0.25) | (1.19) | (0.34) | (1.80) | (0.75) |
| Interaction (Ms2*Poverty per capita (mov. avg.)) | -10.68 | -17.91 | -46.44 | -39.08 | -59.13 | -12.74 | -4.54 | -3.49 | 5.12 | -2.56 |
|  | (1.45) | (1.71) | (4.04) | (2.25) | (0.73) | (2.85) | (1.36) | (1.46) | (1.34) | (0.11) |
| Interaction (Ms3*Population Density) | -0.04 | -0.09 | 0.06 | -0.25 | -0.22 | 0.31 | -0.37 | 0.01 | -0.12 | 1.86 |
|  | (0.94) | (1.39) | (0.78) | (2.33) | (0.43) | (3.48) | (5.43) | (0.23) | (1.49) | (3.92) |
| Interaction (Ms3*Unemployment per capita) | -214.06 | 189.51 | 226.98 | -183.75 | -4301.96 | -48.70 | 410.48 | $155.04$ | -613.46 | 612.73 |
|  | (1.75) | (1.09) | (1.19) | (0.64) | (3.22) | (0.10) | (1.17) | (0.62) | (1.53) | (0.25) |
| Interaction (Ms3*Poverty per capita (mov. avg.)) | 61.48 | -648.15 | 72.00 | -19.35 | 1599.32 | 146.72 | -250.18 | 143.78 | -105.42 | -1560.50 |
|  | (0.86) | (6.37) | (0.64) | (0.11) | (2.04) | (1.17) | (2.66) | (2.14) | (0.98) | (2.35) |

CA means Cash Assistance, M means Payments to Medicaid, NSS means Non-Health Social Services, PH means Public Hospital Spending, and NSWS means Non-Social Welfare Spending.


[^0]:    ${ }^{1}$ See McGuire (1978) and Appendix A for details.
    ${ }^{2}$ In this formulation, the price effects of federal grants induced by matching ratios is not explicitly modeled.

[^1]:    own sources. However, either matching formulas or restrictions can reduce or eliminate this displacement effect. Federal matching serves as a "carrot," rewarding states that spend more in designated areas, while restrictions act as a "stick," taking away funds if the conditions (e.g. maintenance of effort) are not met.

